

**UNIVERSIDADE ESTADUAL DO NORTE FLUMINENSE DARCY RIBEIRO**

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**AVALIAÇÃO QUANTITATIVA DE PERFIS DE CRESCIMENTO DE CAPRINOS MACHOS  
CASTRADOS**

**CAMPOS DOS GOYTACAZES**

**2014**

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Tese apresentada ao Centro de Ciências e Tecnologias Agropecuárias da Universidade Estadual do Norte Fluminense Darcy Ribeiro, como requisito para obtenção do grau de Doutor em Ciência Animal na Área de Concentração em Nutrição e Produção Animal.

ORIENTADOR Prof<sup>o</sup>. D.Sc. Ricardo Augusto Mendonça Vieira

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**Aprovada em 27 de janeiro de 2014.**

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**(Orientador)**

Dedico esta tese à minha família, em especial a  
minha mãe Luizeni, meu pai Juarez, meu irmão  
Leandro e a minha noiva Talita, que sempre  
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## RESUMO

**Araujo, Raphael Pavesi, D.Sc., Universidade Estadual do Norte Fluminense Darcy Ribeiro. Janeiro de 2014. Avaliação quantitativa de perfis de crescimento de caprinos machos castrados. Professor Orientador: Ricardo Augusto Mendonça Vieira.**

O objetivo com este estudo foi caracterizar o crescimento corporal e a composição do corpo vazio de caprinos machos castrados de raças leiteiras em um período longo de crescimento. Os animais foram abatidos ao nascimento (dia zero), e próximos às idades de 15, 90, 135, 210, 270, 365, 485, 610, 735, 790, 840, 890 e 920 dias. Todas as partes do corpo foram pesadas, amostradas e determinados seus constituintes químicos em matéria seca, proteína bruta, gordura bruta, cinzas e energia específica. Os modelos de crescimento Richards, Gompertz e o bifásico Brody-Gompertz foram ajustados para os perfis de crescimento com as diferentes estruturas de variância e covariância (homogênea, exponencial e assintótica) e foram todos avaliados pelo critério de máxima verossimilhança. A eliminação dos outliers melhoraram a probabilidade de verossimilhança de alguns modelos, de forma que diferenças notáveis puderam ser observadas no ponto de inflexão, taxa de crescimento e na tendência das variáveis estudadas. A existência de um ponto de inflexão verdadeiro para muitas variáveis estudadas foi duvidosa, embora o modelo de Richards tenha sido a melhor escolha para descrever a maioria dos perfis avaliados. O modelo bifásico não superou o modelo de Richards, em termos de probabilidade, provavelmente devido ao fato de que o ponto de inflexão relativo à puberdade se confundiu com o efeito da desmama, e pela falta de informações no intervalo entre 15 e 90 dias. De forma geral, os padrões de crescimento exibidos pelas partes do corpo e constituintes químicos foram alométricos em relação a  $W$ . Este comportamento alométrico resultou em diferentes tendências assintóticas: algumas partes do corpo ou componentes químicos atingiram a maturidade mais cedo do que outras. Portanto, o crescimento das partes corporais e a composição do ganho de corpo vazio ao longo do tempo em caprinos castrados não foram constantes em toda a gama de massa corporal estudada.

**Palavras-chave:** Análises de crescimento, Caprino, Máxima verossimilhança, Modelos matemáticos.

## ABSTRACT

**Araujo, Raphael Pavesi, D.Sc., Universidade Estadual do Norte Fluminense Darcy Ribeiro; January 2014; Quantitative assessment of growth of goat wethers profiles. Adviser: Ricardo Augusto Mendonça Vieira.**

The goal of this study was to characterize the growth of body parts and composition of the growing empty body to infer how these aspects relate to the long-term growth of goat wethers from dairy breeds. In addition to birth (day zero) and to 15 days of age, the animals were slaughtered at ages close to 90, 135, 210, 270, 365, 485, 610, 735, 790, 840, 890, and 920 days. All body parts were weighed and sampled to determine chemical constituents dry matter, crude protein, crude fat, ash, and specific energy. The Richards, Gompertz, and a biphasic model formed by the combined Brody and Gompertz growth functions were fitted to the growth profiles with different variance functions and were all evaluated by means of likelihood criteria. The elimination of outliers enhanced the likelihood probability ( $w_r$ ) of some models. Remarkable differences can be noticed regarding inflection points, growth rates, and trends for the variables studied. The existence of a true inflection point for many variables studied was dubious, although the Richards model was the best choice to describe many growth profiles. The biphasic model did not supplant the Richards model in terms of likelihood, and the suspicious additional inflection point prior to the point about puberty due to a transient weaning period lacks data of sufficient quantity between 15 and 90 days of age for an adequate characterization. Generally, the growth patterns exhibited by the body parts and chemical constituents were allometric with respect to  $W$ . This allometric behaviour yielded different asymptotic trends: some body parts or chemical constituents reached maturity earlier than others did. Therefore, growth of body parts and composition of gain in the growing empty body of the goat wethers were not constants in the entire range of body mass studied.

**Keywords:** Growth analysis, Goats, Mathematical models, Maximum likelihood

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## 1. INTRODUÇÃO

Crescimento e desenvolvimento de ruminantes têm sido discutidos e revisados por muitos anos. Vários autores têm especulado ou modelado a taxa e composição do acréscimo de tecido pela idade cronológica, pela idade fisiológica (tamanho adulto, maturidade), pelo consumo de energia, pelo status hormonal, pelo turnover ou renovação relativa dos tecidos e pelo número de células (Owens et al., 1995)

Crescimento usualmente pode ser definido como a produção de novas células, porém, devido ao crescimento ser medido rotineiramente como incremento em massa, pode-se incluir não somente a multiplicação de células (hiperplasia), mas também o aumento do tamanho das células (hipertrofia). Durante o crescimento embrionário, todos os tecidos crescem por hiperplasia, mas em mamíferos adultos as células especializadas (células musculares esqueléticas e tecido adiposo) perdem sua habilidade em se replicar e crescem somente por hipertrofia ou incorporação de células satélites. No entanto, outros tecidos, como precursores de células sanguíneas, folículo capilar, epitélio gastrintestinal, órgãos do trato digestivo, entre outros continuam a se dividir por toda a vida (Owens et al., 1993).

Nem toda porção do corpo se desenvolve igualmente ou ao mesmo tempo durante o crescimento, este crescimento diferenciado por parte do corpo é chamado de desenvolvimento que ocorre do estágio embrionário até a maturidade. Um exemplo bastante corriqueiro é que a cabeça de todos os animais compreende uma maior porção do peso ao nascimento, do que em qualquer estágio posterior da vida, porém o aumento pós-natal é menor que outras partes do corpo (Boggs e Merkel, 1993).

Da antológica obra de Brody (1945), pode-se depreender que o crescimento difere do desenvolvimento pelo fato de este obedecer a uma diretriz biológica; isto é, o crescimento “orquestrado” geneticamente desde a sua concepção à maturidade. O crescimento, dentro desta lógica biológica, ou seja, determinado pela herança e pelas restrições do meio, constitui desenvolvimento. O crescimento, por seu turno, se traduz por síntese biológica, isto é, a produção de novas unidades bioquímicas. É o aspecto do desenvolvimento relacionado aos processos de multiplicação celular, expansão celular e a incorporação de matéria colhida do meio-ambiente. Contudo, o crescimento pode não implicar desenvolvimento; nos tumores, por exemplo, há o crescimento sem função de

diferenciação. O desenvolvimento é o processo de consolidação da heterogeneidade biológica que constitui os seres vivos, particularmente aquele verificado nos animais superiores. Dessa forma, a exigência e a eficiência energética dos animais variam de acordo com o estágio fisiológico.

O estudo do processo de transferência de energia em animais e o mecanismo regulatório envolvido são usualmente definidos como bioenergética. A bioenergética pode ser estudada por vários caminhos, dentre eles, destacam-se: 1- transferências de energia que ocorrem em pequenas etapas químicas, comumente investigados por bioquímicos; 2 - aspectos neurais ou hormonais, que são tratados pelos fisiologistas; 3 - previsão da demanda energética do animal como um todo e a habilidade de diferentes alimentos em satisfazer esta exigência, estes, investigados por nutricionistas (Blaxter,1962).

A utilização da energia pelos animais depende de vários fatores, os quais irão determinar a eficiência da utilização do alimento pelo animal. Em termos termodinâmicos, a eficiência energética de crescimento refere-se à relação do desempenho do crescimento com a energia livre despendida. Tradicionalmente, entretanto, a eficiência energética de crescimento é definida pela relação da energia armazenada no organismo e energia consumida (Brody, 1945).

## 2. REVISÃO DE LITERATURA

### 2.1 CURVA DE CRESCIMENTO

O crescimento e o desenvolvimento são processos complexos fundamentais na vida dos seres vivos. Em síntese, o crescimento animal está relacionado com o aumento de massa e volume, o que determina o tamanho corporal, enquanto o desenvolvimento está envolvido com a diferenciação dos componentes corporais.

Diversos fatores podem influenciar o crescimento de cabritos jovens, desde o nascimento até idades mais avançadas, podendo ser destacados: o peso ao nascimento, sexo e o ganho de peso. O peso ao nascimento indica o desenvolvimento intrauterino do animal, o qual está diretamente relacionado com fatores genéticos, número de animais por parto e a nutrição da cabra durante o período de gestação.

O ganho de peso pode ser definido, basicamente, como o resultado entre o genótipo e o ambiente oferecido ao animal. Os trabalhos na literatura têm apontado grande variação entre os ganhos de peso diário de caprinos durante o crescimento, sendo relatada uma faixa de 45 a 190g dia<sup>-1</sup> para as raças especializadas na produção leiteira. Oliveira (2001) relatou que, em geral, os melhores ganhos de peso na espécie caprina foram observados no período compreendido entre o nascimento e os 5,5 meses de idade, o que evidencia o maior desempenho dos animais nesta fase de produção. Em suma, Fisher (1975) relatou que o aporte alimentar que os animais recebem é determinante para o ritmo de crescimento do animal e, conseqüentemente, para o peso corporal final.

Os principais componentes que influenciam no peso de um animal são os tecidos ósseo, muscular, visceral e adiposo. No processo de crescimento o animal apresenta incremento do peso corporal devido ao acúmulo destes referidos tecidos, respeitando certa ordem de prioridade. Assim, o processo de crescimento animal influencia a seguinte ordenação no desenvolvimento dos tecidos: nervoso, ósseo, muscular e adiposo. Por esta razão, a composição corporal altera-se ao longo do tempo em decorrência das diferentes velocidades de crescimento e maturação dos tecidos (ALLEN et al., 1979; OWENS et al. 1993).

Segundo Fitzhugh Jr. (1976), as curvas de crescimento refletem as inter-relações entre o impulso individual do animal recém-nascido para crescer e atingir a maturação de todas as partes do corpo e o ambiente no qual este impulso se expressa. Owens et al. (1993) sugeriram que o crescimento animal ocorre de forma acelerada na fase inicial, reduzindo com o avanço da idade, sendo que sua respectiva curva apresenta ponto de inflexão associado à puberdade. Os melhores índices de ganho de peso e de conversão alimentar são obtidos pelos animais em crescimento, aproximadamente quando o animal atinge 30% do peso adulto. Taylor, (1985) enfatizou que a obtenção de resultados econômicos positivos na produção animal está, portanto, na dependência do melhor aproveitamento da fase inicial de crescimento.

O interesse no estudo de curvas de crescimento que possa descrever toda a vida do animal já existe há mais de um século (FRANCE et al. 1996). Na tentativa de descrever a curva de crescimento dos animais adequadamente, iniciou-se a utilização de modelos matemáticos não lineares. Uma das primeiras tentativas em descrever o crescimento através de funções matemáticas foi realizada por Quetelet, em 1835, sendo o primeiro a fazer analogias entre as diferentes fases do crescimento de um organismo e a propor uma curva sigmoide para descrevê-lo.

O conhecimento preciso da taxa de crescimento, grau de maturidade e tamanho à maturidade, entre outras características correlacionadas, podem ser obtidas a partir das curvas de crescimento. Tais informações podem constituir interessante ferramenta no processo de tomada de decisões para aumentar a eficiência do rebanho, com destaque para a seleção dos melhores animais para a reprodução, a otimização de dietas apropriadas para suprir as diferentes exigências nutricionais ao longo do desenvolvimento dos animais, a redução dos custos e dos riscos da exploração e o ponto ideal (produtivo e econômico) de abate dos animais.

Para Fitzhugh Jr. (1976), os dados de peso e idade tomados em diferentes períodos de crescimento podem ser chamados de dados longitudinais. A análise dessas medidas repetidas mostra-se de grande importância na produção animal, possibilitando que indivíduos de diferentes subpopulações ou tratamentos (sexo, raça, entre outros) sejam analisados ao longo de diferentes condições de avaliação (tempo, doses, etc.).

A utilização de curvas de crescimento que relacionam o peso do animal à sua idade tem despertado o interesse de muitos pesquisadores em diversas áreas. Para McManus et al. (1997), uma das principais vantagens de utilizar modelos matemáticos

para descrever o crescimento é a consolidação das informações contidas em dados de peso-idade dentro de parâmetros biologicamente interpretáveis.

Poucos estudos sobre curva de crescimento têm sido desenvolvidos no Brasil, estando estes escassos trabalhos concentrados nas áreas de bovinocultura, suinocultura e avicultura. A utilização de modelos matemáticos para descrever a curva de crescimento da espécie caprina é muito recente e conta com número reduzido de publicações.

Esta informação é confirmada por Malhado et al. (2008), em que diz que o número de publicações com caprinos utilizando os modelos de curvas de crescimento é muito reduzido (FREITAS, 2005; OLIVEIRA et al., 2009).

## 2.2 MODELOS MATEMÁTICOS

Os principais modelos matemáticos utilizados na descrição do crescimento dos animais domésticos de interesse zootécnico são: Brody ou monomolecular, Von Bertalanffy, Gompertz, Logístico e Richards (BROWN et al., 1976; FITZHUGH Jr., 1976; OLIVEIRA et al., 2000; MAZZINI et al., 2003; FREITAS, 2005). Segundo Richards (1959), o estudo de curvas de crescimento iniciou com o modelo de Von de Bertalanffy em experimentos sobre metabolismo. France et al. (1996) caracterizaram as funções de crescimento dividindo-as em dois tipos: simples e conjugadas. Dentre as funções simples são destacados os modelos de Brody, Von Bertalanffy, Gompertz e Logístico. A função de Richards é classificada como uma função conjugada.

Segundo Guedes et al. (2004), alguns requisitos devem ser seguidos para que uma função de crescimento seja descrita como uma relação peso-idade. Entre eles destacam-se: (a) a interpretação biológica dos parâmetros (confiabilidade); (b) o ajuste com pequenos desvios (precisão); e (c) o grau de dificuldade do ajuste (operacionalidade do processo).

Sarmiento et al. (2006) reportaram que, uma vez escolhido o modelo que melhor se ajusta ao padrão de crescimento, os parâmetros que o descreve devem ser estudados para identificar os fatores que podem influenciá-los, como raça, sexo, tipo de

nascimento, época e ano de nascimento e idade da mãe ao parto, e possibilitar ajustes no padrão de crescimento.

### 2.2.1 Modelo Brody

O modelo da curva de crescimento pode ser dividido em dois segmentos principais: o primeiro como a fase de aumento da velocidade de crescimento (autoaceleração); e o segundo como a fase de diminuição da velocidade (autoinibição) do crescimento. A passagem de uma fase para outra é marcada por um ponto de inflexão, o qual marca a posição em que o aumento da velocidade de crescimento cessa e a diminuição da velocidade de crescimento ainda não iniciou, sugerindo que o crescimento neste ponto é linear. Neste ponto, o ganho de peso é mais eficiente e mais econômico. Na ausência de forças inibitórias, a taxa de crescimento tenderia a permanecer constante.

France et al. (1996) citaram que o modelo de Brody teve como norte o estudo monomolecular desenvolvido por Spillman e colaboradores para avaliar a lei dos retornos decrescentes para descrever o peso corporal de um animal como uma função do seu consumo de alimentos. Assim, utilizou-se este modelo em conjunção com o modelo exponencial para contabilizar a forma de “S” exibida pelos padrões de crescimento de populações, animais e outros organismos ao longo do tempo.

Segundo Doren et al. (1989), o modelo de Brody foi inicialmente utilizado para descrever o crescimento animal ocorrido após o ponto de inflexão. Entretanto, seu uso não está restrito à fixação dos valores iniciais. Assim, considera-se o nascimento como ponto de inflexão, que pode ser aplicado para descrever todo o crescimento pós-natal.

A taxa de crescimento relativo instantâneo pode ser obtida pela equação:

$$k = \left( \frac{dW}{dt} \right) / W \quad \text{equação 1}$$

onde,

$k$  é a taxa relativa de crescimento instantâneo;

$dW$  é o diferencial do peso;



$dt$  é o diferencial do tempo;

$W$  é o peso no instante em que  $dW/dt$  foi medido.

No entanto, com a dificuldade de medir o ganho instantâneo, utilizou-se um método de integração para modificar a equação de  $dW/dt = kW$  para

$$W_t = W_0 e^{kt} \quad \text{equação 2}$$

em que,

$W$  é o peso acumulado no tempo  $t$ ;

$W_0$  é o peso inicial;

$k$  é a taxa de crescimento específica.

Linearizando a equação 2, tem-se:

$$\ln W_t = \ln W_0 + kt \quad \text{equação 3}$$

No entanto, as equações 2 e 3 só se mostraram adequadas por um período inicial do crescimento. O autor relata que a taxa de crescimento declina com o aumento da idade, mantendo-se relativamente constante em determinados intervalos de tempo. O declínio da taxa de crescimento é muito mais lento do que antes (não parecendo ser constante) e depois declina de forma relativamente abrupta a um novo nível mais baixo. Brody (1945) teoriza que o ponto de inflexão da curva, onde a aceleração seria zero, estaria relacionado a um momento de mudança fisiológica, que ocorre em todos os animais, a puberdade.

Para a elaboração de uma equação que represente a fase de inibição do crescimento após a inflexão da curva, segundo o autor, pode-se também utilizar o princípio de ação das massas. Ao invés da taxa de crescimento ser proporcional ao tamanho do animal, ela agora será proporcional à disponibilidade de alimentos, à retirada de produtos deletérios ao crescimento, ou a qualquer elemento que se mostre limitante. Se o suprimento de alimento limitante é necessário para atingir o máximo tamanho individual ( $A$ ) e  $W$  o fornecimento de alimento até um dado tempo, então  $A-W$  representa a concentração do alimento limitante, que permite atingir o máximo tamanho individual.

Para Brody (1945), é razoável assumir que a velocidade de crescimento instantânea,  $dW/dt$ , em um dado momento será proporcional ao fornecimento da concentração de alimentos limitante ( $A - W$ ):

$$dW/dt = -k(A - W) \quad \text{equação 4}$$

onde, o sinal negativo atribuído ao  $k$  indica o declínio da velocidade de crescimento.

Portanto, de maneira geral, os valores numéricos das constantes são estimados como:  $A$ , representando a concentração do fator limitante de crescimento, quando o crescimento é completamente inibido, podendo ser usada para representar o peso à maturidade do animal;  $W$  pode representar o peso do animal em um dado tempo;  $A - W$  representa, então, o crescimento ainda a ser realizado para atingir o peso à maturidade.

Integrando-se a equação 4 tem-se (FRANCE et al., 1996):

$$W = A - Be^{-kt} \quad \text{equação 5}$$

em que,

$B$  é a diferença  $A - W_0$ ;

$k$  é a taxa de crescimento relativa ao crescimento a ser realizado.

A constante  $B$  é empregada para corrigir o fato de que, embora a idade seja contada a partir do nascimento ou concepção, a equação 5 ajusta os dados somente durante a fase de crescimento posterior à inflexão da curva. O expoente  $k$  é o declínio da velocidade de crescimento em taxa constante.

Brody (1945) enfatiza que as duas equações utilizadas para descrever o crescimento (2 e 5), poderiam ser combinadas em uma única equação,  $dW/dt = kW(A - W)$ . Porém, tal equação (com adição de constantes ou não), segundo o autor, não representa o ciclo todo de crescimento dos animais apresentando quebras na curva de crescimento e irregularidades similares no crescimento de populações. Portanto, Brody (1945) optou por descrever o crescimento a partir de duas equações (2 e 5) que explicassem as fases de aceleração e inibição do crescimento.

### 2.2.2 Modelo Gompertz

A função Gompertz, desenvolvida originalmente em 1825, utiliza a taxa de inibição proporcional ao logaritmo desta variável, ou seja, a taxa de crescimento é grande no início do processo, mudando rapidamente para um crescimento mais lento (SCAPIM, 2008). Segundo Laird (1965), tal função foi apontada como própria para a

descrição do crescimento dos organismos vivos, com base no argumento de que a capacidade média de crescimento, medida pela velocidade relativa de aumento, tende a cair em uma taxa mais ou menos uniforme, conduzindo a tipos assimétricos de curvas sigmóides.

Seguindo o mesmo raciocínio, France et al. (1996) descreveram o modelo de Gompertz com um comportamento sigmóidal suave, sem descontinuidade. E com a efetividade do crescimento diminuindo ao longo do tempo de acordo com a cinética de primeira ordem.

Para Fialho (1999), a função de Gompertz tem propriedades desejáveis como modelo de curva de crescimento, principalmente pelo fato de considerar que a massa corporal inicial é sempre superior à zero, o que reflete o fato de que o animal já nasce com alguma massa.

A função Gompertz proposta por Laird (1965) e citada por Ludwig (1977) tem a seguinte forma:

$$w_t = w_0 \exp(k(1 - \exp(-Dt))/D) \quad \text{equação 6}$$

Onde,  $w_0$  = massa inicial;  $k$  = taxa de crescimento específica;  $D$  = taxa de redução fracional do crescimento.

Ainda segundo France et al. (1996), a taxa de crescimento relativo instantâneo ou a primeira derivada pode ser expressa da seguinte forma:

$$\frac{dy_t}{dt} = k \exp -dt \times w_0 \exp(k(1 - \exp(-Dt))/D) \quad \text{equação 7}$$

### 2.2.3 Modelo Richards

France et al. (1996) expuseram que o modelo de Richards, por ser determinado como função conjugada, engloba as funções simples de crescimento (Brody, Bertalanffy, logística e Gompertz), conferindo uma generalidade que é frequentemente útil para descrever o crescimento animal.

Em seu trabalho “Uma função de crescimento flexível para uso empírico”, Richards retoma considerações de Von Bertalanffy (1957) como a relação alométrica de crescimento entre a taxa metabólica do animal e seu peso, afirmando que a inclinação

(n) da linha alométrica é de 2/3 para espécies obedecendo à lei de superfície do metabolismo. Richards também retoma a afirmação de que a taxa de anabolismo é proporcional ao peso elevado a *m-ésima* potência, mas a taxa de catabolismo é proporcional ao próprio peso. Assim a taxa de crescimento em peso, dada pela diferença entre anabolismo e catabolismo, é dada por:  $\eta W^n - kW$ , onde  $\eta$  e  $\kappa$  são constantes de anabolismo e catabolismo, respectivamente. Quando  $m=1$ ,  $dW/dt = (\eta - k)W$  o crescimento é exponencial. Para baixos valores de  $n$  a integração leva a equação de crescimento a seguir (FRANCE et al.,1996):

$$\mu_{Y_t} = Y_0 \times Y_f / (Y_0^m + (Y_f^m - Y_0^m) \exp(-kt))^{1/m} \quad \text{equação 8}$$

Onde,  $Y_0$  = massa inicial;  $Y_f$  = massa final;  $m$ = escalonamento da massa;  $k$ = taxa de crescimento relativo;  $t$ = tempo.

Richards afirmou que embora seja interessante, a derivação da taxa de crescimento contém algumas considerações que colocam em dúvida sua validade teórica; além disso, valores de  $m$  acima de 1 são rejeitados, não por nunca ocorrerem, mas provavelmente pela necessidade teórica de manter  $\eta$  e  $\kappa$  em uma variação numérica compatível com sua interpretação como constantes de anabolismo e catabolismo, respectivamente. Tal fato pode ser facilmente comprovado pelo uso de  $m > 1$ , já que os valores de  $\eta$  e  $\kappa$  seriam negativos.

Uma vez que a equação 8 proporciona resultados irrealistas de  $m$  e  $k$  em situações nas quais  $m > 1$ , ela foi reescrita para:

$$W^{1-m} = A^{1-m} - \beta e^{-kt}$$

Em que  $A^{1-m}$ ,  $\beta$  e  $k$ , são constantes:

$$A^{1-m} = (\eta/k), \beta = \eta/k W_0^{(1-m)} = A^{1-m} - W_0^{(1-m)}, ek = (1 - m)k$$

Posteriormente foi reparametrizada para:

$$W^{1-m} = A(1 \pm b e^{-kt}) \quad \text{equação 9}$$

Em que  $b = \pm \beta A^{1-m}$ , onde o sinal é negativo quando  $m < 1$  e positivo quando  $m > 1$ .

Neste sentido a curva de crescimento de Richards (1959) descreve mudanças no tamanho  $W$  (peso) em relação à idade  $t$ , representada como:

$$W_t = A(1 - b e^{-kt})^m \quad \text{equação 10}$$

O modelo Richards considera que o ponto de inflexão das curvas é variável, mesmo que dentro de uma mesma população. Isto ocorre devido à relevância do parâmetro  $m$ , que é relativo à forma da curva, com ponto de inflexão variável. Assim,

dependendo do valor de  $m$ , a função de Richards pode apresentar as formas das outras funções de ponto de inflexão fixo. Desta forma, dependendo do valor do parâmetro  $m$  na equação 10, tem-se:

Brody	$W = A(1 - be^{-kt})$	( $m = 0$ )
Von Bertalanffy	$W = A(1 - be^{-kt})^3$	( $m = 2/3$ )
Logístico	$W = A/(1 + be^{-kt})$	( $m = 2$ )
Gompertz	$W = Ae^{-be^{-kt}}$	( $m > 1$ )
Richards	$W = A(1 - be^{-kt})^m$	( $m$ variável)

Em resumo, quando  $0 < m < 1$ , tem-se um modelo intermediário entre o de Brody e Gompertz; quando  $1 < m < 2$ , o formato se situa entre o modelo de Gompertz e o modelo Logístico; quando  $m > 2$  o resultado é um modelo similar ao logístico, porém assimétrico, em que o ponto de inflexão pode ser alterado para um valor maior do que  $W = A/W$ .

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#### 4. CAPITULO 1

O CAPITULO 1 APRESENTADO A SEGUIR FOI SUBMETIDO PARA PUBLICAÇÃO NO PERIÓDICO “THE JOURNAL OF AGRICULTURAL SCIENCE” (ISSN:0021-8596; IMPACT FACTOR: 1.691), DE MODO QUE O MESMO FOI EDITADO CONFORME AS NORMAS ESPECÍFICAS DESTE PERIÓDICO, QUE PODEM SER OBTIDAS NO SEGUINTE ENDEREÇO ELETRÔNICO: [http://assets.cambridge.org/AGS/AGS\\_ifc.pdf](http://assets.cambridge.org/AGS/AGS_ifc.pdf)



1     **Growth of goat wethers from birth to maturity: quantitative description of the growing**  
2                                   **body, body parts, and composition of gain**

3  
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26 **Summary**

27 The goal of this study was to characterize the growth of body parts and composition of  
 28 the growing empty body to infer how these aspects relate to the long-term growth of  
 29 goat wethers from dairy breeds. In addition to birth (day zero) and to 15 days of age, the  
 30 animals were slaughtered at ages close to 90, 135, 210, 270, 365, 485, 610, 735, 790,  
 31 840, 890, and 920 days. All body parts were weighed and sampled to determine  
 32 chemical constituents dry matter, crude protein, crude fat, ash, and specific energy. The  
 33 Richards, Gompertz, and a biphasic model formed by the combined Brody and Gompertz  
 34 growth functions were fitted to the growth profiles with different variance functions and  
 35 were all evaluated by means of likelihood criteria. The elimination of outliers enhanced  
 36 the likelihood probability ( $w_r$ ) of some models. Remarkable differences can be noticed  
 37 regarding inflection points, growth rates, and trends for the variables studied. The  
 38 existence of a true inflection point for many variables studied was dubious, although the  
 39 Richards model was the best choice to describe many growth profiles. The biphasic  
 40 model did not supplant the Richards model in terms of likelihood, and the suspicious  
 41 additional inflection point prior to the point about puberty due to a transient weaning  
 42 period lacks data of sufficient quantity between 15 and 90 days of age for an adequate  
 43 characterization. Generally, the growth patterns exhibited by the body parts and  
 44 chemical constituents were allometric with respect to  $W$ . This allometric behaviour  
 45 yielded different asymptotic trends: some body parts or chemical constituents reached  
 46 maturity earlier than others did. Therefore, growth of body parts and composition of  
 47 gain in the growing empty body of the goat wethers were not constants in the entire  
 48 range of body mass studied.

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50 **Keywords:** Growth analysis, Goats, Mathematical models, Maximum likelihood

51 **Introduction**

52           Mathematical functions have been used to describe growth of domestic  
53 ruminants for predictive purposes, and the information can be used at both scientific  
54 and farm levels. Nonlinear models are mathematical functions that are nonlinear in its  
55 parameters. Parameters do not belong to the real world but they are useful as  
56 representations of reality, they are ideally computed from random samples taken  
57 unbiasedly for point and interval estimation of the same parameters that are inferred to  
58 the population of interest. Parameters of traditional growth functions are empirical and  
59 can be aggregated, for instance, at the organismal level; they summarize information  
60 about the growth profile into a few parameters such as the specific growth rate and  
61 weights at birth and maturity in addition to a homoscedastic residual variance.  
62 Whenever detected in the growth profile, the inflection point is usually attributable to  
63 puberty, the point at which sexual maturity begins and the growth rate starts to reduce  
64 asymptotically to zero. Nonetheless, progress in computation statistics have been  
65 introduced into statistical software that allow a more general quantitative description of  
66 growth by generalizing not only the expected growth but also the variance about growth  
67 trends, thus accommodating heteroscedasticity and co-variation at both between and  
68 within individuals including repeated records as time advances.

69           The growth of ruminants is centripetal, which means that head and foreparts  
70 achieves asymptotic growth prior to inner body counterparts (Lawrence & Fowler  
71 2002). However, goat wethers, like other castrated farm ruminants, probably grow  
72 further in length of long bones compared to intact animals, but hormones other than  
73 oestrogen and testosterone may act as determinants of complete ossification of  
74 epiphyseal plates after puberty (Doumit & Merkel 2005; Hossner 2005). In general,  
75 weight records of ruminants resemble a sigmoid-shaped pattern, and body parts such as

76 bones, muscles, and fat exhibit remarkable differences in their growth profiles; besides,  
77 maturity of these major body constituents occurs earlier for bones, intermediate for  
78 muscles, and later for fat with reference to the timing for body maturing (Doumit &  
79 Merkel 2005).

80         The growth of body mass of castrated male goats can be described by the  
81 Richards (1959) model because of the flexible nature of this model for fitting a myriad of  
82 growth profiles (France et al. 1996; López et al. 2000). Nevertheless, how body parts  
83 and body composition change from birth to maturity in goats? The distribution of fat in  
84 the body of goats differ from other ruminant species, and visceral fat accretion is a  
85 striking characteristic that may help goats to survive and even produce in the face of  
86 seasonal food shortages (Carmichael et al. 2012). Despite the fact that castrates usually  
87 have intermediary growth profiles if compared to intact males and females, information  
88 gathered may be of use for predictive purposes. Therefore, the goal of this study was to  
89 characterize the growth of body parts and composition of the empty body to infer how  
90 these aspects relate to the long-term growth of goat wethers from specialized dairy  
91 breeds.

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101 **Material and methods**

102 Alpine (chamois) and Saanen kids used in the present study were sampled from  
103 the annual offspring of a large dairy herd raised in the county of Viçosa (20°46'22" S,  
104 42°51'12" W, and elevation 706 m), Zona da Mata Region, State of Minas Gerais (Brazil),  
105 where predominates a Cwa climate according to the Köppen standards. Two Saanen and  
106 two Alpine kids were slaughtered at birth and at 15 days old, one Saanen and three  
107 Alpine kids were slaughtered. Afterwards, 50 kids (37 Alpine and 13 Saanen) were  
108 moved to be raised in the county of Campos dos Goytacazes (21°42'36" S, 41°20'22" W,  
109 and elevation 15 m), northern Rio de Janeiro state, where an Aw climate predominates  
110 and the kids were castrated immediately after their arrival.

111 The kids were reared in a floor-bed type barn until weaning at 90 d. A milk  
112 replacer was fed, and a soybean meal and grounded corn mixture was offered to the  
113 animals on a daily basis. Cunhã (*Clitoria ternatea* L.), Elephant-grass (*Pennisetum*  
114 *purpureum*, Schum.), and occasionally, Sabiá (*Mimosa caesalpiniiifolia*, Bentham) were  
115 the roughages available and offered ad libitum to the kids until weaning. After 90 days,  
116 the kids were transferred to a stilted-type barn with slatted floor and the animals  
117 received a ration based on soybean meal, grounded corn, minerals, and Mayze silage  
118 (*Zea mays*, L.). Additional roughage was offered (Cunhã, Elephant-grass, and  
119 occasionally Sabiá) ad libitum according to the availability of forages. The diet was  
120 formulated for a target average daily weight gain of 0.150 kg/day (AFRC 1997), and was  
121 adjusted over time according to the availability of forage.

122 In addition to birth (day zero) and to 15 days of age, the animals were  
123 slaughtered at ages close to 90, 135, 210, 270, 365, 485, 610, 735, 790, 840, 890, and  
124 920 days. Nonetheless, the growth profiles were obtained with the actual age at  
125 slaughter for each animal to avoid bias. The oldest age at slaughter was chosen at the

126 time of replacement of the last deciduous incisive teeth. Four animals were slaughtered  
 127 at each age, excepting the last age when six animals were slaughtered. Half of the  
 128 animals were slaughtered two hours after the morning meal and the other half two  
 129 hours after the afternoon meal to measure the contents of the full gastrointestinal tract.  
 130 At slaughter, the animals were rendered insensible, bled, flayed, and eviscerated.  
 131 Individual parts, i.e., the head, members, half carcasses, blood, skin, organs (including  
 132 the remaining of reproductive tract and bladder), the segments of the gastrointestinal  
 133 tract and their contents, total abdominal fat (omental, pelvic, and renal), and trimmed  
 134 cuts (diaphragm, non-carcass muscle pieces, and thymus) were weighed to the nearest  
 135 0.005 kg. All body parts, including carcass, head, and members were grounded in a  
 136 cutting mill.

137 The body parts were dried at 55°C, and except for blood and skin samples, the  
 138 excess fat from body parts was prior removed by petroleum ether extraction in large  
 139 volume (500 ml) Soxhlet apparatus. The defatted samples were ball-milled and their dry  
 140 matter (*DM*, method 967.03; AOAC, 1998), crude protein (*CP*, method 2001.11; Thiex et  
 141 al., (2002)), crude fat (*CF*, method 2003.06; Thiex et al. (2003)), and ashes (*Ash*;  
 142 method 942.05; AOAC (1998)) contents were determined. Another exception was the  
 143 abdominal fat that undergone all chemical analysis without prior ball-milling. The  
 144 energy content of the body was computed from the caloric equivalents of protein and  
 145 fat, i.e., 23.4 and 39.3 MJ/kg, respectively (Maynard et al. 1979). The *DM*, *CP*, *CF*, *Ash*,  
 146 and energy contents were computed in the empty body weight (*EBW*), namely *EBDM*,  
 147 *EBCP*, *EBCF*, *EBAsh*, and *EBE*. The water content of the *EBW* was computed as  
 148  $EBH_2O = EBW - EBDM$ .

149 The general structure attributed to the growth models was  $Y_t \sim Normal(\mu_{Y_t}, \sigma_{Y_t}^2)$ ,  
 150 and the form of the mean ( $\mu_{Y_t}$ ) and variance ( $\sigma_{Y_t}^2$ ) are as follows:

151  $\mu_{Y_t} = Y_0 \exp(k(1 - \exp(-Dt))/D);$  Eqn (1)

152  $\mu_{Y_t} = Y_0 \times Y_f / (Y_0^n + (Y_f^n - Y_0^n) \exp(-kt))^{1/n}$  Eqn (2)

153  $\mu_{Y_t} = Y_{f1} - (Y_{f1} - Y_{10}) \exp(-k_1 t) + Y_{20} \exp(k_2(1 - \exp(-Dt))/D);$  Eqn (3)

154  $\sigma_{Y_t}^2 = \sigma^2;$  Eqn (4)

155  $\sigma_{Y_t}^2 = \sigma_0^2 \exp(ct);$  Eqn (5)

156  $\sigma_{Y_t}^2 = \sigma_0^2 + \sigma_b^2(1 - \exp(-st)).$  Eqn (6)

157 The Eqn (1) is the Gompertz model and its parameters  $Y_0$ ,  $k$ , and  $D$  are the intercept  
 158 (mass units), specific growth rate ( $\text{days}^{-1}$ ), and fractional reduction rate of the specific  
 159 growth rate ( $\text{days}^{-1}$ ), respectively. The Richards model or Eqn (2) is the general model  
 160 used as a reference for describing growth (Richards 1959). In Eqn (2),  $Y_0$  is the  
 161 intercept,  $Y_f$  is the asymptotic growth parameter,  $k$  is the specific growth rate, and  $n$  is a  
 162 size-scaling-related parameter that could be constrained, for instance, by the metabolic  
 163 body size. The monomolecular or Brody growth model is combined with the Gompertz  
 164 model to form the biphasic function shown by Eqn (3), in which  $Y_{f1}$  is a scale parameter  
 165 (mass units) representing the asymptotic phase of the monomolecular growth phase,  $Y_{10}$   
 166 is the scale intercept (mass units), and  $k_1$  ( $\text{days}^{-1}$ ) is the specific growth rate of the first  
 167 order initial growth. The parameter  $Y_{20}$  (mass units) is a scale parameter representing  
 168 the intercept of the sigmoid phase of growth, and  $k_2$  and  $D$ , both expressed as  $\text{days}^{-1}$ ,  
 169 are the specific growth rate and its fractional rate of reduction during the sigmoid  
 170 growth phase, respectively. The variances was modelled as follows: homogeneous  
 171 variances ( $\sigma^2$ ) as shown by Eqn (4); as exponential variances or Eqn (5), in which  $\sigma_0^2$   
 172 represents the starting variance associated to weights at birth ( $t = 0$ ) that increases  
 173 exponentially during growth at a fractional rate  $c$  ( $\text{days}^{-1}$ ); and as an asymptotically  
 174 growing variance or Eqn (6), in which  $\sigma_0^2$  is the variance related to weights at birth,  $\sigma_b^2$  is

175 the asymptotic increase in variance over time, and  $s$  ( $\text{days}^{-1}$ ) is the fractional rate or  
 176 first-order rate of increase in the variance. Therefore, nine models were fitted to the  
 177 growth profiles: the Gompertz model or Eqn (1) associated to Eqn (4), Eqn (5), or Eqn  
 178 (6); Eqn (2) combined with Eqns (4), (5), or (6); and the Brody-Gompertz model or Eqn  
 179 (3) combined with Eqns (4), (5), or (6), respectively.

180 The nine models were fitted to the growth profiles by using the nonlinear mixed  
 181 models procedure (NLMIXED) of SAS (v.9, SAS Systems, Inc., Cary, NC, USA). The chosen  
 182 Newton-Raphson algorithm solved the maximum likelihood estimation method.  
 183 Absolute residuals (observed minus predicted values) and 95% confidence intervals  
 184 (95% *CI*) for the predicted growth were requested as an additional output. A residual  
 185 analysis was performed to detect outliers common to the nine models fitted. An  
 186 individual observation was considered as an outlier whenever its absolute residual  
 187 exceeds three times the absolute value of the half amplitude of the 95% *CI* for the  
 188 respective predicted value. Those observations that shared common residuals to all  
 189 models were removed from the original dataset. In sequence, the models were fitted  
 190 again and likelihood criteria were computed to evaluate the quality of fit of the nine  
 191 models. The corrected Akaike information criterion (Akaike 1974; Sugiura 1978) is an  
 192 output of the SAS System. The derived likelihood criteria were computed as follows  
 193 (Burnham & Anderson 2004):

$$194 \quad \Delta_r = AICc_r - \min AICc_r; \quad \text{Eqn (7)}$$

$$195 \quad w_r = \exp(-\Delta_r/2) / (\sum_{r=1}^9 \exp(-\Delta_r/2)); \quad \text{Eqn (8)}$$

$$196 \quad ER_r = (\max w_r) / w_r. \quad \text{Eqn (9)}$$

197 The corrected Akaike criterion, namely  $AICc_r$ , computed for the  $r$ -th model in the set of  
 198 nine models was used to calculate the differences ( $\Delta_r$ ) between the  $r$ -th model and the  
 199 minimum (min)  $AICc_r$  computed in the set of nine models fitted (Eqn (7)). In Eqn (8)  $w_r$



200 is the likelihood probability computed for the  $r$ -th model fitted in the set. In Eqn (9)  $ER_r$   
 201 is the evidence ratio computed from the maximum (max)  $w_r$  in the set of models fitted  
 202 and the respective  $w_r$  value of  $r$ -th fitted model under evaluation. Models that presented  
 203  $0 \leq \Delta_r \leq 2$  also presented higher  $w_r$  and lower  $ER_r$  values, and therefore were  
 204 considered the best choice giving the data. Models with  $2 < \Delta_r \leq 8$  were considered to  
 205 have less support, and models with  $\Delta_r > 8$  were considered the worse choices among  
 206 models. The number of parameters was considered as an additional parsimony criterion  
 207 whenever the models were equally likely, and the model with a smaller number of  
 208 parameters was preferably chosen. A fully estimated correlation matrix and parameters  
 209 different from zero were considered additional distinguishing criteria indicative of a  
 210 well-conditioned model.

211           Once chosen the two models that most likely fit each growth profile the original  
 212 residuals obtained after the first fit of the two models were inspected again to identify  
 213 possible outliers. After the elimination of the outliers to both models, they were fitted  
 214 again and their quality of fit was assessed by the same likelihood criteria described by  
 215 Eqns (7), (8), and (9).

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225 **Results**

226           Because of the lack of information between 15 and 90 days, the estimation of the  
227 variance of the parameter  $k_1$  of Eqn (3) presented numerical problems and did not  
228 converge into a limit, i.e., tended to infinity. All of the remaining parameters of this  
229 equation presented plausible point and interval estimates. Therefore, to fit this equation  
230 more properly, the starting value for  $k_1$  was fixed at one.

231           Some variables were fitted in grams (g) and other variables were fitted in kg  
232 because scale interfered in convergence during the optimization process. The  
233 likelihoods were categorized and only those models that presented  $\Delta_r < 6$  after the first  
234 fit are shown in Table 1. This multimodel selection was performed first to eliminate  
235 models that presented no support in mimicking the growth profiles. In sequence, the  
236 likelihoods of the two models that best fitted to the growth profiles are presented in  
237 Table 2.

238           The plot of the absolute residuals for some variables were presented as an  
239 additional information to illustrate the performance of some models studied by  
240 contrasting the worse and the better choices in mimicking data (Fig. 1). In the first case  
241 presented (*W*), the resulting fit of Eqn (2) combined with Eqn (5) (panel b) is compared  
242 to Eqn (3) combined with Eqn (4) (panel a). In the second case (*AbFat*), the worst  
243 choice would be Eqn (1) fitted under the assumption of homoscedasticity (Eqn (4))  
244 (panel c), whereas the best choice was Eqn (1) fitted to data assuming Eqn (6) (panel d).  
245 Clearly, in the case of *AbFat*, the residual variability increases over time, thus indicating  
246 that the homoscedastic assumption did not hold true. In the third case (*Carcass*), the  
247 same improvement of fit can be noted because the variance increased exponentially  
248 (Eqns (2) and (5)) (panel f), and apparently the Richards-Exponential model mimicked  
249 the growth profile better than Eqn (3) fitted under the assumption of homogeneity

250 (panel e). The fourth case was presented to illustrate the improved fit of combined Eqns  
 251 (2) and (5) (panel h) in relation to the fit of combined Eqns (3) and (4) (panel g),  
 252 because the former presents a more even distribution of the residuals than the latter  
 253 and accounted for an exponential increase in the variances over the time interval  
 254 studied.

255 The elimination of outliers enhanced the likelihood probability ( $w_r$ ) of some  
 256 models, and it can be saw by contrasting likelihood measures from Tables 1 and 2 (e.g.,  
 257 the combined Eqns (2) and (5) for describing  $W$  and  $EBW$ ). The Gompertz model or Eqn  
 258 (1) was unequivocally the best choice for six of the 16 variables studied, thus indicating  
 259 a pure sigmoid behaviour for organs (*Organs*), gastrointestinal tract (*GIT*), skin (*Skin*),  
 260 abdominal fat (*AbFat*), trimmed cuts (*Trimcut*), and ruminoreticular contents (*RRC*).  
 261 This means that the additional parameter of Eqn (2) did not improved the fit of the  
 262 Richards model to highly sigmoid growth profiles. The other 10 variables, namely body  
 263 weight ( $W$ ), empty body weight ( $EBW$ ), carcass weight (*Carcass*), blood (*Blood*), fresh  
 264 weight of the gastrointestinal tract contents (*GITC*), the dry matter content of the empty  
 265 body (*EBDM*), and the empty body ash (*EBAsh*), crude fat (*EBCF*), crude protein  
 266 (*EBCP*), and energy (*EBE*) had their growth profiles best mimicked by Eqn (2) (Table  
 267 2). Despite the major influence of the sigmoid growth pattern of *AbFat* (Fig. 2g) over the  
 268 *EBE* (Fig. 3h), i.e., the former was better described by Eqn (1), the Richards model or  
 269 Eqn (2) was the best choice for describing the energy retained in the empty body of the  
 270 castrated male goats.

271 In terms of variance, a homogeneous model or Eqn (4) was more likely for *RRC*;  
 272 an exponential model or Eqn (5) was the best choice for describing  $W$ ,  $EBW$ , *Carcass*,  
 273 *Skin*, *Blood*, *EBDM*, *EBAsh*, and *EBCP*; whereas an asymptotic variance trend was more

274 likely to describe the variability about *Organs*, *GIT*, *AbFat*, *Trimcut*, *GITC*, *EBCF*, and  
 275 *EBE* (Table 2).

276 The estimated  $\hat{\mu}_{Y_t}$  and  $\hat{\sigma}_{Y_t}^2$  for each variable are presented in Table 3. Graphs were  
 277 built to illustrate point and interval estimates for  $\mu_{Y_t}$  in the continuum of the time-axis  
 278 (Figs. 2 and 3). One can note that visually well-defined asymptotes were reached for  
 279 variables of Fig. 2, excepting *EBW* in panel (b) and *Carcass* in panel (c). The same can  
 280 be said about variables *EBDM* (panel d), *EBCF* (panel f), and *EBE* (panel h) of Fig. 3  
 281 because a well-defined asymptotic phase was not apparent. In Figs. 2 and 3 are also  
 282 displayed the 95% *CI* of the intercept and asymptote of the variables indicating masses  
 283 at birth and at maturity. Some limits of the growth functions yielded plausible estimates  
 284 at maturity; nonetheless, as mentioned before, some asymptotic values were  
 285 overestimated, thus indicating that, for some variables, weights at maturity were less  
 286 likely and a well-defined asymptote had not been reached (e.g., *EBDM* in Fig. 3d).

287 The age of the animals from birth to maturity (approximately at 900 days) was  
 288 categorized into six age classes to better illustrate the average daily gain in *W*, *EBW*,  
 289 *EBCP*, *EBCF*, and *EBE* at these stages of growth. As such, one can draw some interesting  
 290 results from Table 4. For instance, the protein and energy gain in the *EBW* can be  
 291 estimated. Between 90 and 210 days of age, the average daily rate of net protein  
 292 retention, i.e.,  $\Delta EBCP / \Delta t$ , divided by the average daily rate of gain in the *EBW*, i.e.,  
 293  $\Delta EBW / \Delta t$ , is  $1000 \times 0.015 / 0.106 = 142 \text{ g} \cdot \text{kg}^{-1}$ . The same approach can be used to  
 294 compute the net rate of energy retention, i.e., at the same age interval,  $1.456 / 0.106 =$   
 295  $13.736 \text{ MJ} \cdot \text{kg}^{-1}$  of *EBW*. One can calculate the limits of the confidence intervals in the  
 296 same way.

297 Other relevant relationships about observed and predicted body composition as  
 298 functions of the predicted empty body weight and amount of crude protein retained in

299 the empty body weight were drawn (Fig. 4). The behaviour of *EBCP*, *EBF*, and *EBE*  
 300 remained nonlinear with respect to the predicted *EBW* (Fig. 4, panels a, b, and d). The  
 301 exception was the nearly linear behaviour exhibited by *EBAsh* as a function of the  
 302 predicted *EBW*. The increase in the retained crude protein was similar to a diminishing  
 303 returns trend, whereas the fat and energy contents appears to have increased  
 304 exponentially within the *EBW* interval studied; the *EBAsh* appears to have increased at  
 305 a constant rate in relation to *EBW* because it resembles a linear increase (Fig. 4c). The  
 306 fat, energy, and ash amounts in the empty body augmented in an exponential-like  
 307 fashion as the predicted crude protein amount in the empty body increased (Fig. 4,  
 308 panels e, f, and g). Nevertheless, the water amount in the empty body (*EBH<sub>2</sub>O*)  
 309 increased in an almost linear fashion as the predicted *EBCP* increased (Fig. 4h). A  
 310 simple no intercept linear regression model was fitted by means of ordinary least  
 311 squares (PROC REG of SAS) to the data pairs (*W*, *EBW*), and a constant *EBW/W* ratio of  
 312  $92.58 \pm 1.51$  kg/100 kg was estimated with an adjusted  $R^2 = 0.9776$ .

313 Generally, the growth patterns exhibited by the body parts and chemical  
 314 constituents were allometric with respect to *W*. Remarkable differences can be noticed  
 315 regarding inflection points, growth rates, and trends for the variables studied (Figs. 2  
 316 and 3, and Table 5). The existence of a true inflection point for many variables studied  
 317 was dubious, although the Richards model was the best choice to describe many growth  
 318 profiles (Table 2). Table 5 contains large confidence intervals that were estimated for  
 319 the age at the point of inflection for Eqn (2): negative estimates indicate no inflection  
 320 during the postnatal life of the animal; there were no reason for rejecting the hypothesis  
 321 that  $t_i = 0$  for *W*, *Carcass*, and *EBCP*; and despite the variability the point of inflection  
 322 for *EBW* was detectable. The applicability of the weights at the inflection lacks  
 323 generality for *W* and *Carcass* in which, clearly, the large confidence intervals did not

324 exclude  $t_i = 0$ ; for *Blood* and *EBCP* is nonsense to compute a predicted weight at the  
 325 points of inflection ( $\hat{Y}_{t_i}$ ) for negative  $t_i$ . For all other variables of Table 5, the existence of  
 326 an inflection point was likely and, therefore, also likely the existence of a predictable  
 327 weight at the point of inflection. The weight of body, body parts, and chemical  
 328 constituents of the empty body at the point of inflection of *EBW* were presented in  
 329 Table 5 to illustrate the rates of mass gain and its ratio between weight at 142.9 days  
 330 and the weight at 900 days, i.e., close to maturity. In this regard, for instance, one can  
 331 calculate the mass ratio between this two time points for the protein amount of the  
 332 body:  $100 \times 3.3/9.7 = 34.02\%$  of the mature protein mass was deposited about 5  
 333 months of age. The animals reached 30.66% of the mature weight at the inflection point  
 334 of *EBW*.

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349 **Discussion**

350           The examination of residuals have been used for evaluating the quality of fit of  
351 regression models (Draper & Smith 1966; Bard 1974; Motulsky & Cristopoulos 2003;  
352 Strathe et al. 2010). Departures from randomness in the plots of the residuals obtained  
353 after fitting the models characterized by combining Eqns (1)–(3) and Eqns (4)–(6) were  
354 difficult to distinguish; to the eye, the examination of the residuals was insufficient as a  
355 tool for model selection in the present study. For all examples illustrated (Fig. 1) and  
356 other variables studied (not shown), residuals presented evenly distributed patterns  
357 irrespective of the model used. Other measures used to judge the quality of fit of  
358 different nested and non-nested models, such as the  $F$ -ratio test and  $R^2$  would not be  
359 effective. In fact,  $F$ -ratio brings the dichotomy about rejecting or not rejecting the null  
360 hypothesis and do not provide a reasonable basis for testing multiple hypotheses or  
361 multi-model selection (Burnham & Anderson 2004; Stang et al. 2010), and the  $R^2$  or  
362 adjusted  $R^2$  were inherited from linear models and its computation was not even  
363 mentioned or said to be necessary according to the specialized literature about  
364 nonlinear models, e.g., Bard (1974), Ratkowsky (1990), and Pinheiro and Bates (2000).  
365 Therefore, approaches that are more robust are recommended for such cases. Provided  
366 that the sample is representative of the population, i.e., data gathered represent the  
367 truth, the Akaike information criterion (Akaike 1974) corrected for samples of smaller  
368 sizes or  $AIC_c$  (Sugiura 1978) and its derived measures as additional information  
369 criteria (Burnham & Anderson 2004) have been used efficiently to assess the likelihood  
370 of different linear and nonlinear models in a multiple-hypotheses framework (Wolfinger  
371 1993; Motulsky & Cristopoulos 2003; Burnham & Anderson 2004; Vieira et al. 2012).

372           The theory related to nonlinear mixed models allows establishing relationships  
373 among a dependent variable and a set of independent variables in a general way not

374 constrained by linear functions. A nonlinear mixed model is a general mathematical  
375 function built on parametric constants or parameter functions with physical or  
376 biological meaning to which fixed and random effects that may influence parameters of  
377 the general nonlinear relationship are introduced. The structure is completed with an  
378 additional model that represent the variation between and within experimental units  
379 (subjects or individuals) that accommodate both correlations among repeated measures  
380 taken over time on the same individual and heteroscedasticity between and, whenever  
381 pertinent, within individuals. To complete this framework, the artefact parameters can  
382 be estimated by the method of maximum likelihood that further provides additional  
383 measures of the strength of evidence that the model mimics the real world (McCulloch &  
384 Searle 2001; Littell et al. 2006; Vonesh 2012). An important feature of this framework is  
385 the possibility to model variation assuming a multivariate normal distribution of the  
386 parameters among individuals (Brunel et al. 2013). There are some examples in the  
387 literature in which the variance-covariance structures are modelled by accommodating  
388 correlated errors among longitudinal data and accounting for a general exponential  
389 increase in the variance over time (Littell et al. 2006; Strathe et al. 2010; Vonesh 2012).  
390 In this study, for those variables in which a well-defined asymptotic phase was not  
391 evident, the exponential model or Eqn (5) mimicked the variability of the growth  
392 profiles and resulted in a better description of the variance increase over time, just like  
393 the same way as Littell et al. (2006), Strathe et al. (2010), and Vonesh (2012) reported.  
394 Nonetheless, some variables presented a distinguishable asymptotic phase, and this  
395 well-established attribute of the growth profile was probably associated to an  
396 asymptotic variance increase over time, as modelled in the form of Eqn (6). The two  
397 patterns described by Eqns (5) and (6) are departures from the homoscedasticity  
398 assumption. The exception was the description of the growth of the ruminoreticular



399 contents because of the high variability of homoscedastic nature recorded throughout  
 400 the time profile (Fig. 3c). The definition of the asymptotic growth phase is crucial to  
 401 establish the weights and its variability at maturity, particularly for vertical production  
 402 systems that host breeding categories, as still is the case of goat dairying systems. Only  
 403 experiments that last long enough to characterize maturity allow a proper estimation of  
 404 the asymptotic weights (Blaxter et al. 1982; France et al. 1996; Strathe et al. 2010);  
 405 otherwise, smaller time-trend effects jeopardize inferences regarding asymptotic  
 406 weights (Strathe et al. 2010).

407 Several nonlinear models have been applied to describe the growth of farm  
 408 animals (France et al. 1996; López et al. 2000; Marinho et al. 2013; Souza et al. 2013),  
 409 and their parameter estimates are inferred to the population of interest by averaging out  
 410 temporary environmental effects and by accounting for the nonlinear effect of time  
 411 (Brown et al. 1976). However, there are events and processes that may constrain the  
 412 growth trajectory such as weaning, puberty, maturation, seasonal food availability and  
 413 quality (Morand-Fehr 1981; Brunel et al. 2013; Magistrelli et al. 2013) interfering  
 414 directly in the orchestrated genetic plan of growth, which demand nonconventional  
 415 approaches for its quantitative description. Therefore, multiphasic nonlinear models  
 416 may be useful for interpreting growth profiles that present more than one detectable  
 417 inflection points, i.e., additional inflection points to the one related to puberty because of  
 418 constraints to growth impinged by the environment may retard or accelerates the rate  
 419 of weight gain (Koops 1986; Nesetrilova 2005; Mendes et al. 2008; Rocha 2013). Some  
 420 growth profiles presented in this study stand the reasonable doubt of an additional  
 421 inflection point close to the earliest ages (0–90 days) perceptible by visual appraisal  
 422 after the enlargement of the time scale. The biphasic model described by Eqn (3) was  
 423 employed by Rocha (2013) to characterize the transition from the suckling phase to a

424 solid diet and subsequent weaning as an additional constraint that introduces another  
 425 inflection point to the growth profile of castrated male kids. Nonetheless, the biphasic  
 426 model or Eqn (3) did not supplant the Richards model or Eqn (2) in terms of  
 427 likelihood, and the suspicious additional inflection point prior to the point about puberty  
 428 due to the transient weaning period lacks data of sufficient quantity between 15 and 90  
 429 days of age for an adequate characterization. Although puberty is not strictly applicable  
 430 to wethers, puberty in specialized dairy goat breeds occurs between 90–120 days when  
 431 the growth rate starts to decrease and may be confounded with weaning effects due to  
 432 the close proximity of these two events in time (Morand-Fehr 1981; Rocha 2013). In this  
 433 study, the age at inflection for the empty body weight (*EBW*) occurred later than 120  
 434 days (Table 5). Somehow, the high variability observed for gut contents at earlier ages  
 435 and long-term nonlinear effects of time over the gut contents might have affected the  
 436 estimated precocious age at the inflection point for *W*, despite the constant ratio  
 437 observed between *EBW* and *W*.

438         Some postnatal growth profiles resembled the first-order or monomolecular  
 439 growth traditionally described by the law of diminishing returns (Figs. 2 and 3), as  
 440 Brody (1945) pointed out as the self-inhibiting growth phase. This can be attributed to  
 441 the fact that the inflection point has had occurred during the kid's prenatal life. In fact, a  
 442 Gompertz-like model have been applied to anticipate the growth of kids during prenatal  
 443 life (AFRC 1993; 1997). Therefore, self-accelerating phase occurring during prenatal  
 444 growth and self-inhibiting phase initiating nearby birth or soon after birth may be a  
 445 clear indicative of the large variation about the age at the point of inflection observed for  
 446 *W* in Table 5. Therefore, Eqn (3) or the Richards (1959) model was unequivocally  
 447 superior in terms of likelihood to describe a self-inhibiting-like profile because the

448 referred model has a flexible nature that mimics growth patterns such as those  
 449 described by the Brody's model (France et al. 1996; López et al. 2000).

450 Describing growth as a simple sequence of self-accelerating followed by self-  
 451 inhibiting processes may be an oversimplification; even after adding an intermediary  
 452 phase as the linear logarithmic phase to represent a tripartite description of growth can  
 453 be considered an oversimplification. It is worthy to remember that models are fitted to  
 454 the growth patterns and empirically aggregate into a few parametric constants the  
 455 thermodynamically unfavourable and complex biochemical growth phenomena (Brody  
 456 1945; Lawrence & Fowler 2002). The sigmoid pattern of growth is the integrated sum of  
 457 the growth rates of many body parts (Owens et al. 1993). As taught by France et al.  
 458 (1996), there are growth rates that can be described empirically by a first-order growth  
 459 or  $dY/dt = k(Y_f - Y)$ . Sigmoid models mimic growth profiles that may be attributed to  
 460 a gradual reduction of the fractional growth rate at birth, i.e.,  $dY/dt = Yk \exp(-Dt)$ , that  
 461 yields the Gompertz model or Eqn (1). The general model built by Richards (1959)  
 462 owes its general nature to fit monomolecular or sigmoid profiles due to the assumed  
 463 growth rate  $dY/dt = kY(Y_f^n - Y^n)/(nY_f^n)$ , that generalizes the balance between  
 464 catabolic and anabolic processes scaled to the body proper suggested by von Bertalanffy  
 465 (1957). Biphasic models can be introduced to deal with an asymptotic first-order  
 466 growth combined with sigmoid growth so that  $dY/dt = k_1(Y_{f1} - Y) + Yk_2 \exp(-Dt)$ ;  
 467 the first-order growth occurs primarily during the birth-weaning period and the sigmoid  
 468 growth after the weaning shock (Rocha 2013). This latter model is not constrained by  
 469 any break point; it mimics empirically the net result of simultaneously growing body  
 470 parts with different timings. Nonetheless, due to the reduced influence of short-term  
 471 effects upon a more complete time profile for animals growing up to maturity (Strathe et

472 al. 2010), and for the sake of statistical rigour, Eqn (3) was considered not likely for  
 473 representing the growth of goat wethers.

474         The growing animal faces seasonal changes in the environment. As it grows upon  
 475 an unlimited food supply, growth is mainly constrained by genotype and daily intake  
 476 rate will stabilize at maturity (Blaxter et al. 1982; Lawrence & Fowler 2002). Generally,  
 477 after puberty, there are expenditures of nutrients for maintenance, somatic growth, and  
 478 reproduction (including lactation) that shall be balanced by rate of nutrient intake  
 479 (Brunel et al. 2013). The growth condition for does achieves this complexity, because  
 480 well managed does still grow after first kidding and reach their variable mature size only  
 481 after the second kidding (Morand-Fehr 1981). For castrates, a balance between nutrient  
 482 acquisition and expense may explain stabilization of growth (Blaxter et al. 1982), but the  
 483 reproductive cycle constrain doelings and bucklings as they grown into adulthood.  
 484 Blaxter et al. (1982) theorized that maturity weight is achieved when nutrient intake  
 485 and expenditure reach a balance because long-term intake at maturity as well as body  
 486 composition reach a steady-state condition. This condition does not mean that maturity  
 487 weight is immutable; but rather is the balance between maintenance and reproductive  
 488 expenditures, as well as efforts for harvesting nutrients from the environment  
 489 (Lawrence & Fowler 2002).

490         The long-term profiles studied here by extending the *EBW* range from birth to  
 491 maturity revealed a nonlinear behaviour for the body composition (Fig. 4). The result  
 492 was that body parts grew in an allometric fashion as demonstrated by different ages at  
 493 the points of inflection (Table 5) and by different growth patterns (Figs. 2, 3, and 4).  
 494 This allometric behaviour yielded different asymptotic trends: some body parts or  
 495 chemical constituents reached maturity earlier than others did. Therefore, growth of  
 496 body parts and composition of gain in the growing empty body of the goat wethers were

497 not constants, i.e.,  $dY/dEBW \neq \beta$ , for  $\beta$  representing a dimensionless constant. Blaxter  
 498 et al. (1982) observed a linear increase for the lipid mass in the empty body of sheep,  
 499 but they studied a narrower *EBW* range, i.e., from 40 to 120 kg as those authors focused  
 500 on the post-puberal phase of growth. The linear relationships for *EBash* and *EBW* and  
 501 for water in the empty body (*EBH<sub>2</sub>O*) and *EBCP* observed by Blaxter et al. (1982) for  
 502 sheep also appears to have had occurred for goat wethers. Other relationships reported  
 503 here were nonlinear (Fig. 4) if compared to the growth behaviours reported by Blaxter  
 504 et al. (1982). The rate of fat deposition in does is larger than in wethers, which in turn is  
 505 larger than in bucks; in addition, differences are more remarkable at heavier body  
 506 weights (Mahgoub et al. 2004). Crossbreds of Alpine × Hair, and Saanen × Hair goats  
 507 have heavier carcass weights and internal fat weights than Hair breeds (Gokdal 2013).  
 508 Carmichael et al. (2012) argued that adult dairy goats (Saanen) probably have more  
 509 carcass fat than younger ones. By taking weights at 900 and 142.9 days from Table 5, the  
 510 difference *EBCF* – *AbFat* was 13.6 and 1.7 kg of non-abdominal fat for adults and  
 511 younglings, respectively, what represented non-abdominal fat contents of 18.63 and  
 512 9.24 kg/100 kg of *EBW* for the respective categories. The adipose tissue grows by both  
 513 hypertrophic and hyperplastic mechanisms (Hossner 2005). Therefore, an unrestricted  
 514 food supply may explain the absence of an asymptotic phase for *EBCF* profile in Fig. 3f,  
 515 in which the predicted asymptote was higher than the predicted value at 900 days of  
 516 age. As the growth rate of the animal increases the accretion rate of fat increases and  
 517 protein decreases (NRC 2007); this was confirmed by results shown in Tables 4 and 5  
 518 that also confirmed the fact that fat and protein contents in the empty body respectively  
 519 increase and decrease as wethers mature (Tedeschi et al. 2010). Nonetheless, given the  
 520 scarcity of information regarding body composition of goats (NRC 2007), the obtained  
 521 estimates of chemical composition of wethers (Tables 3, 4, and 5) can be ad interim used

522 to predict net energy and protein deposition in the empty body of females, at least for  
523 ages not greater than 210 days; for older ages, reproduction hampers generalizations.

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Table 1. Likelihood of the models fitted\* to the growing body, body parts, and chemical composition of the body of castrated male goats.

Variable	Model	$AICc_r^\dagger$	$\Delta_r^\dagger$	$w_r^\dagger$	$ER_r^\dagger$	$\theta_r^\dagger$
$W^\ddagger$ (kg)	Eqns (2), (5)	292.1	0.0	0.922	1	6
	Eqns (2), (6)	297.8	5.7	0.053	17	7
$EBW^\ddagger$ (kg)	Eqns (2), (5)	330.0	0.0	0.988	1	6
Carcass (kg)	Eqns (2), (5)	259.8	0.0	0.811	1	6
	Eqns (2), (6)	265.5	5.7	0.047	17	7
	Eqns (3), (5)	263.9	4.1	0.104	8	8
Organs (g)	Eqns (1), (6)	671.3	0.0	0.712	1	6
	Eqns (2), (6)	673.4	2.1	0.249	3	7
$GIT^\ddagger$ (g)	Eqns (3), (6)	725.5	0.0	0.981	1	9
Skin (g)	Eqns (1), (4)	684.6	2.2	0.137	3	4
	Eqns (1), (5)	682.4	0.0	0.412	1	5
	Eqns (1), (6)	683.9	1.5	0.195	2	6
	Eqns (2), (5)	684.0	1.6	0.185	2	6
$AbFat^\ddagger$ (g)	Eqns (1), (5)	860.9	5.0	0.063	12	5
	Eqns (1), (6)	855.9	0.0	0.770	1	6
	Eqns (3), (6)	859	3.1	0.163	5	9
$Trimcut^\ddagger$ (g)	Eqns (1), (6)	621.7	0.0	0.646	1	6
	Eqns (2), (6)	622.9	1.2	0.354	2	7
Blood (kg)	Eqns (2), (5)	719.6	0.0	0.854	1	6
	Eqns (3), (6)	723.7	4.1	0.110	8	9
	Eqns (1), (6)	912.4	0.0	0.550	1	6
$GITC^\ddagger$ (g)	Eqns (2), (6)	912.8	0.4	0.450	1	7
	Eqns (1), (4)	654.8	0.0	0.919	1	4
$RRC^\ddagger$ (g)	Eqns (1), (6)	660.2	5.4	0.062	15	6
	Eqns (2), (5)	242.5	0.0	0.851	1	6
$EBDM^\ddagger$ (kg)	Eqns (2), (6)	246.40	3.9	0.121	7	7
	Eqns (1), (5)	-24.1	0.3	0.428	1	5
	Eqns (2), (5)	-24.4	0.0	0.497	1	6
$EBash^\ddagger$ (kg)	Eqns (3), (5)	-19.0	5.4	0.033	15	8
	Eqns (2), (5)	207.0	4.8	0.077	11	6
	Eqns (2), (6)	202.2	0.0	0.850	1	7
$EBCF^\ddagger$ (kg)	Eqns (3), (6)	207.3	5.1	0.066	13	9
	Eqns (2), (5)	94.9	0.0	0.768	1	6
	Eqns (2), (6)	98.4	3.5	0.133	6	7
$EBCP^\ddagger$ (kg)	Eqns (3), (5)	99.8	4.9	0.066	12	8
	Eqns (2), (5)	620.4	0.0	0.475	1	6
	Eqns (2), (6)	620.4	0.0	0.475	1	7
$EBE^\ddagger$ (MJ)	Eqns (3), (6)	625.4	5.0	0.039	12	9

\*Likelihood results obtained after the elimination of common outliers. Details of Eqns (1), (2), (3), (4), (5), and (6) are in the text;

$^\dagger AICc_r$ , corrected Akaike information criterion of the  $r$ -th model;  $\Delta_r$ , difference between the  $AICc_r$  and the minimum of the  $AICc_r$  in the set of all models tested;  $w_r$ , likelihood probability of the  $r$ -th model;  $ER_r$ , evidence ratio against the  $r$ -th model;  $\theta_r$ , number of parameters of the  $r$ -th model including the related variance parameters.

$^\ddagger W$ , body weight;  $EBW$ , empty body weight;  $GIT$ , gastrointestinal tract weight;  $AbFat$ , weight of the abdominal fat;  $Trimcut$ , weight of the trimmed cuts;  $GITC$ , fresh weight of the gastrointestinal contents;  $RRC$ , fresh weight of the ruminoreticular contents; empty body contents of dry matter ( $EBDM$ ), ash ( $EBash$ ), crude fat ( $EBCF$ ), crude protein ( $EBCP$ ), and energy ( $EBE$ ).

Table 2. Likelihood of the two best models fitted\* to the growing body, body parts, and chemical composition of the body of castrated male goats.

Variable	Model	$AICc_r^\dagger$	$\Delta_r^\dagger$	$w_r^\dagger$	$ER_r^\dagger$	$\Theta_r^\dagger$
$W^\ddagger$ (kg)	Eqns (2), (5)	285.0	0.0	0.950	1	6
	Eqns (2), (6)	290.9	5.9	0.050	19	7
$EBW^\ddagger$ (kg)	Eqns (2), (5)	275.3	0.0	0.998	1	6
	Eqns (2), (6)	288.3	13.0	0.002	665	7
$Carcass$ (kg)	Eqns (2), (5)	259.8	0.0	0.886	1	6
	Eqns (3), (5)	263.9	4.1	0.114	8	8
$Organs$ (g)	Eqns (1), (6)	662.1	0.0	0.711	1	6
	Eqns (2), (6)	663.9	1.8	0.289	3	7
$GIT^\ddagger$ (g)	Eqns (1), (6)	652.0	0.0	0.512	1	6
	Eqns (3), (6)	652.1	0.1	0.488	1.1	9
$Skin$ (g)	Eqns (1), (5)	664.4	0.0	0.668	1	4
	Eqns (1), (6)	665.8	1.4	0.332	2	5
$AbFat^\ddagger$ (g)	Eqns (1), (6)	770.9	0.0	0.973	1	5
	Eqns (3), (6)	778.1	7.2	0.027	37	6
$Trimcut^\ddagger$ (g)	Eqns (1), (6)	621.7	0.0	0.646	1	6
	Eqns (2), (6)	622.9	1.2	0.354	2	7
$Blood$ (g)	Eqns (2), (5)	674.8	0.0	0.999	1	6
	Eqns (3), (6)	689.2	14.4	0.001	1339	9
$GITC^\ddagger$ (g)	Eqns (1), (6)	827.8	0.3	0.463	1	6
	Eqns (2), (6)	827.5	0.0	0.537	1	7
$RRC^\ddagger$ (g)	Eqns (1), (4)	625.5	0.0	0.966	1	4
	Eqns (1), (6)	632.2	6.7	0.034	29	6
$EBDM^\ddagger$ (kg)	Eqns (2), (5)	220.4	0.0	0.875	1	6
	Eqns (2), (6)	224.3	3.9	0.125	7	7
$EBAsh^\ddagger$ (kg)	Eqns (2), (5)	-48.9	0.0	0.750	1	6
	Eqns (1), (5)	-46.7	2.2	0.250	3	5
$EBCF^\ddagger$ (kg)	Eqns (2), (6)	184.8	0.0	0.999	1	7
	Eqns (2), (5)	198.6	13.8	0.001	992	6
$EBCP^\ddagger$ (kg)	Eqns (2), (5)	86.8	0.0	0.818	1	6
	Eqns (2), (6)	89.8	3.0	0.182	5	7
$EBE^\ddagger$ (MJ)	Eqns (2), (6)	503.8	0.0	0.999	1	7
	Eqns (2), (5)	517.4	13.6	0.001	898	6

\*Likelihood results obtained after the elimination of common outliers. Details of Eqns (1), (2), (3), (4), (5), and (6) are in the text.

$^\dagger AICc_r$ , corrected Akaike information criterion of the  $r$ -th model;  $\Delta_r$ , difference between the  $AICc_r$  and the minimum of the  $AICc_r$  in the set of all models tested;  $w_r$ , likelihood probability of the  $r$ -th model;  $ER_r$ , evidence ratio against the  $r$ -th model;  $\Theta_r$ , number of parameters of the  $r$ -th model including the related variance parameters.

$^\ddagger W$ , body weight;  $EBW$ , empty body weight;  $GIT$ , gastrointestinal tract weight;  $AbFat$ , weight of the abdominal fat;  $Trimcut$ , weight of the trimmed cuts;  $GITC$ , fresh weight of the gastrointestinal contents;  $RRC$ , fresh weight of the ruminoreticular contents; empty body contents of dry matter ( $EBDM$ ), ash ( $EBAsh$ ), crude fat ( $EBCF$ ), crude protein ( $EBCP$ ), and energy ( $EBE$ ).

Table 3. Computed parameter estimates of the chosen models.

Variable	Model	Mean ( $\hat{\mu}_{Y_t}$ )	Variance ( $\hat{\sigma}_{Y_t}^2$ )
<i>W</i> * (kg)	Eqns (2), (5)	$4.7 \times 94.0 / (4.7^{-0.8926} + (94.0^{-0.8926} - 4.7^{-0.8926}) \exp(-0.002t))^{-1/0.8926}$	$1.9 \exp(0.002t)$
<i>EBW</i> * (kg)	Eqns (2), (5)	$4.7 \times 96.6 / (4.7^{-0.6704} + (96.6^{-0.6704} - 4.7^{-0.6704}) \exp(-0.002t))^{-1/0.6704}$	$1.4 \exp(0.004t)$
<i>Carcass</i> (kg)	Eqns (2), (5)	$3.1 \times 65.1 / (3.1^{-0.8708} + (65.1^{-0.8708} - 3.1^{-0.8708}) \exp(-0.001t))^{-1/0.8708}$	$1.3 \exp(0.003t)$
<i>Organs</i> (g)	Eqns (1), (6)	$317.3 \exp(0.018(1 - \exp(-0.009t))) / 0.009$	$1286.1 + 1.2 \times 10^5 (1 - \exp(-4.6 \times 10^{-4}t))$
<i>GIT</i> * (g)	Eqns (1), (6)	$145.3 \exp(0.035(1 - \exp(-0.013t))) / 0.013$	$81.4 + 5.3 \times 10^4 (1 - \exp(-0.011t))$
<i>Skin</i> (g)	Eqns (1), (5)	$659.6 \exp(0.007(1 - \exp(-0.005t))) / 0.005$	$1.3 \times 10^4 \exp(0.002t)$
<i>AbFat</i> * (g)	Eqns (1), (6)	$64.3 \exp(0.026(1 - \exp(-0.005t))) / 0.005$	$102.7 + 1.8 \times 10^7 (1 - \exp(-8.3 \times 10^{-5}t))$
<i>Trimcut</i> * (g)	Eqns (1), (6)	$56.8 \exp(0.031(1 - \exp(-0.014t))) / 0.014$	$29.9 + 1.4 \times 10^4 (1 - \exp(-0.009t))$
<i>Blood</i> (g)	Eqns (2), (5)	$237.1 \times 2988.0 / (237.1^{-1.000} + (2988.0^{-1.000} - 237.1^{-1.000}) \exp(-0.002t))^{-1/1.000}$	$6.7 \times 10^3 \exp(-0.003t)$
<i>GITC</i> * (g)	Eqns (2), (6)	$103.3 \times 7023.8 / (103.3^{-0.5736} + (7023.8^{-0.5736} - 103.3^{-0.5736}) \exp(-0.011t))^{-1/0.5736}$	$395.2 + 9.0 \times 10^5 (1 - \exp(-0.007t))$
<i>RRC</i> * (g)	Eqns (1), (4)	$215.7 \exp(0.051(1 - \exp(-0.016t))) / 0.016$	$3.0 \times 10^5$
<i>EBDM</i> * (kg)	Eqns (2), (5)	$1.3 \times 60.1 / (1.3^{-0.6376} + (60.1^{-0.6376} - 1.3^{-0.6376}) \exp(-0.002t))^{-1/0.6376}$	$0.3 \exp(0.005t)$
<i>EBAsh</i> * (kg)	Eqns (2), (5)	$0.2 \times 3.8 / (0.2^{-0.5209} + (3.8^{-0.5209} - 0.2^{-0.5209}) \exp(-0.002t))^{-1/0.5209}$	$2.9 \times 10^{-3} \exp(0.004t)$
<i>EBCF</i> * (kg)	Eqns (2), (6)	$0.1 \times 40.2 / (0.1^{-0.4488} + (40.2^{-0.4488} - 0.1^{-0.4488}) \exp(-0.002t))^{-1/0.4488}$	$3.7 \times 10^{-4} + 830.0 (1 - \exp(-1.2 \times 10^{-5}t))$
<i>EBCP</i> * (kg)	Eqns (2), (5)	$0.8 \times 11.7 / (0.8^{-0.9682} + (11.7^{-0.9682} - 0.8^{-0.9682}) \exp(-0.002t))^{-1/0.9682}$	$6.7 \times 10^{-2} \exp(0.003t)$
<i>EBE</i> * (MJ)	Eqns (2), (6)	$22.9 \times 2280.3 / (22.9^{-0.5738} + (2280.3^{-0.5738} - 22.9^{-0.5738}) \exp(-0.001t))^{-1/0.5738}$	$8.3 + 1.0 \times 10^5 (1 - \exp(-1.4 \times 10^{-4}t))$

\**W*, body weight; *EBW*, empty body weight; *GIT*, gastrointestinal tract weight; *AbFat*, weight of the abdominal fat; *Trimcut*, weight of the trimmed cuts; *GITC*, fresh weight of the gastrointestinal contents; *RRC*, fresh weight of the ruminoreticular contents; empty body contents of dry matter (*EBDM*), ash (*EBAsh*), crude fat (*EBCF*), crude protein (*EBCP*), and energy (*EBE*).

Table 4. Average daily rate of retention ( $\Delta\hat{y}_t/\Delta t$ ) of body weight ( $W$ ), empty body weight ( $EBW$ ), body crude protein ( $EBCP$ ), body crude fat ( $EBCF$ ), and body energy ( $EBE$ ).

Age (days)	$\frac{\Delta W/\Delta t^*}{df = 44^\ddagger}$	$\frac{\Delta EBW/\Delta t^*}{df = 49^\ddagger}$	$\frac{\Delta EBCP/\Delta t^*}{df = 42^\ddagger}$	$\frac{\Delta EBCF/\Delta t^*}{df = 43^\ddagger}$	$\frac{\Delta EBE/\Delta t^\dagger}{df = 47^\ddagger}$
0 – 15	0.134 ± 0.036	0.086 ± 0.127	0.019 ± 0.007	0.008 ± 0.003	0.784 ± 0.162
15 – 90	0.133 ± 0.015	0.095 ± 0.010	0.018 ± 0.003	0.016 ± 0.004	1.077 ± 0.168
90 – 210	0.120 ± 0.008	0.106 ± 0.007	0.015 ± 0.002	0.028 ± 0.003	1.456 ± 0.107
210 – 365	0.098 ± 0.008	0.093 ± 0.004	0.012 ± 0.001	0.036 ± 0.002	1.656 ± 0.084
365 – 730	0.064 ± 0.006	0.070 ± 0.009	0.007 ± 0.001	0.034 ± 0.003	1.605 ± 0.164
730 – 900	0.039 ± 0.012	0.047 ± 0.015	0.005 ± 0.002	0.025 ± 0.002	1.269 ± 0.097

\*( $\text{kg}\cdot\text{day}^{-1}$ ).

†( $\text{MJ}\cdot\text{day}^{-1}$ ).

‡ $df$  means denominator degrees of freedom calculated as the number of observations minus the number of parameters in the model.

Table 5. Ages at the inflection point ( $t_i$ , days), predicted values at the estimated  $t_i$  for the variables ( $\hat{Y}_{t_i}$ , g, kg, or MJ) and growth rates ( $d\hat{Y}_{t_i}/dt$ , g, kg, or MJ.day<sup>-1</sup>), and  $\hat{Y}_{t_i}$  and  $d\hat{Y}_{t_i}/dt$  at the estimated point of inflection for the empty body weight ( $t_i = 142.9$  days) and predicted weight of the variables at  $t = 900$  days of age. The acronym NA means not applicable.

Variable <sup>†</sup>	Model <sup>‡</sup>	$t_i$	$\hat{Y}_{t_i}$	$d\hat{Y}_{t_i}/dt$	$\hat{Y}_{t_i=142.9}$	$d\hat{Y}_{t_i=142.9}/dt$	$\hat{Y}_{t=900}$
<i>W</i> (kg)	Eqns (2), (5)	22.6 ± 132.0	7.7 ± 17.6	0.135 ± 0.026	23.3 ± 1.1	0.121 ± 0.018	76.0 ± 3.5
<i>EBW</i> (kg)	Eqns (2), (5)	142.9 ± 105.8	18.4 ± 1.0	0.101 ± 0.007	—	—	73.0 ± 3.9
<i>Carcass</i> (kg)	Eqns (2), (5)	50.1 ± 288.3	6.2 ± 7.2	0.063 ± 0.012	12.0 ± 0.8	0.061 ± 0.006	44.2 ± 2.5
<i>Organs</i> (g)	Eqns (1), (6)	71.0 ± 7.1	793.8 ± 26.8	7.3 ± 0.6	1285.9 ± 54.9	6.1 ± 0.3	2156.6 ± 72.3
<i>GIT</i> (g)	Eqns (1), (6)	77.2 ± 13.0	811.4 ± 35.1	10.5 ± 3.0	1438.9 ± 158.3	8.0 ± 0.5	2205.6 ± 95.3
<i>Skin</i> (g)	Eqns (1), (5)	104.8 ± 15.6	1222.7 ± 56.5	5.6 ± 0.6	1435.4 ± 59.8	5.5 ± 0.5	3238.1 ± 116.6
<i>AbFat</i> (g)	Eqns (1), (6)	347.2 ± 47.6	5374.7 ± 312.7	26.2 ± 1.1	977.1 ± 103.2	12.9 ± 1.4	13654.0 ± 600.5
<i>Trimcut</i> (g)	Eqns (1), (6)	55.6 ± 16.7	189.5 ± 15.9	2.7 ± 0.7	385.9 ± 56.4	1.6 ± 0.3	515.1 ± 43.2
<i>Blood</i> (g)	Eqns (2), (5)	-34.4 ± 10.5	NA	NA	1038 ± 41	4.7 ± 0.3	2673 ± 45
<i>GITC</i> (g)	Eqns (1), (6)	76.4 ± 11.4	2556.3 ± 153.3	8.28 ± 1.52	5211.8 ± 513.7	40.8 ± 9.3	6948.8 ± 416.7
<i>RRC</i> (g)	Eqns (1), (4)	74.0 ± 10.4	1992.8 ± 77.7	31.5 ± 4.0	3868.7 ± 367.6	20.6 ± 1.9	5416.8 ± 211.1
<i>EBDM</i> (kg)	Eqns (2), (5)	229.8 ± 64.7	12.2 ± 3.2	0.053 ± 0.006	7.7 ± 0.5	0.051 ± 0.004	40.5 ± 3.0
<i>EBAsh</i> (kg)	Eqns (2), (5)	198.5 ± 81.3	0.9 ± 0.3	0.004 ± 0.001	0.7 ± 0.05	0.004 ± 0.001	3.0 ± 0.2
<i>EBCF</i> (kg)	Eqns (2), (6)	370.3 ± 48.4	10.6 ± 1.2	0.038 ± 0.003	2.7 ± 0.5	0.028 ± 0.003	27.3 ± 2.5
<i>EBCP</i> (kg)	Eqns (2), (5)	-25.4 ± 227.1	NA	NA	3.3 ± 0.2	0.016 ± 0.002	9.7 ± 0.6
<i>EBE</i> (MJ)	Eqns (2), (6)	347.1 ± 62.7	516.6 ± 30.0	1.681 ± 0.103	187.7 ± 21.5	1.450 ± 0.112	1330.6 ± 59.4

<sup>†</sup>*W*, body weight; *EBW*, empty body weight; *GIT*, gastrointestinal tract weight; *AbFat*, weight of the abdominal fat; *Trimcut*, weight of the trimmed cuts; *GITC*, fresh weight of the gastrointestinal contents; *RRC*, fresh weight of the ruminoreticular contents; empty body contents of dry matter (*EBDM*), ash (*EBAsh*), crude fat (*EBCF*), crude protein (*EBCP*), and energy (*EBE*).

<sup>‡</sup>Details of Eqns (1), (2), (3), (4), (5), and (6) are in the text.

Heading: Prediction of the long-term growth of goat wethers

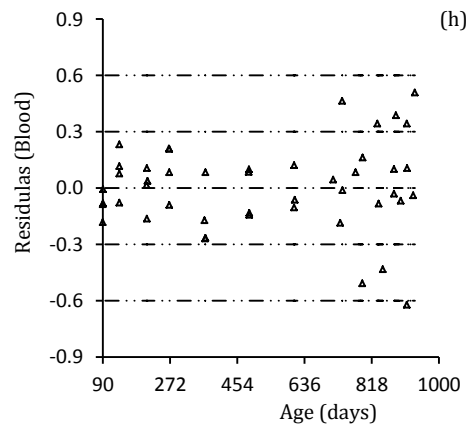
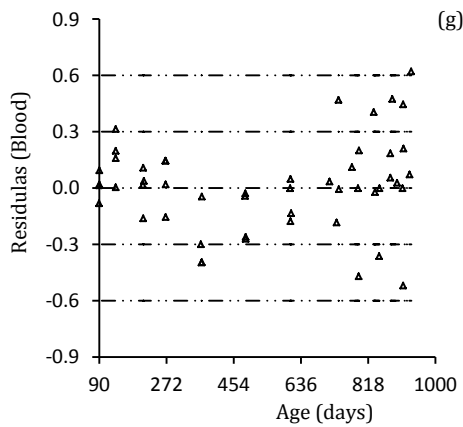
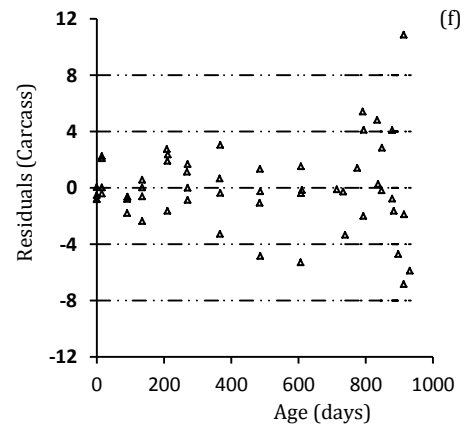
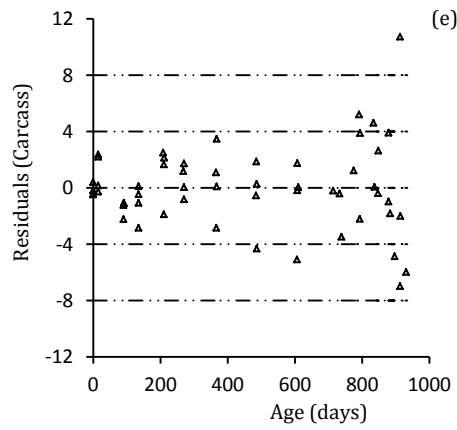
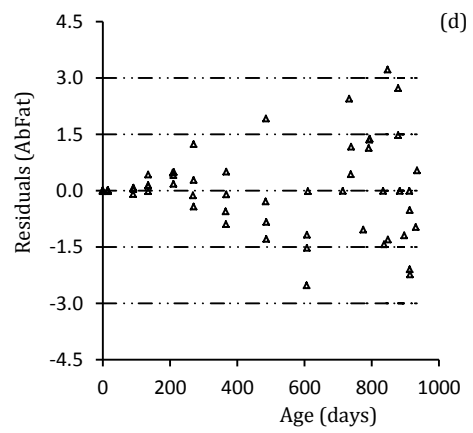
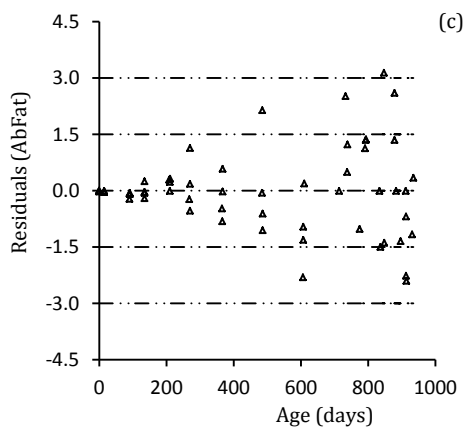
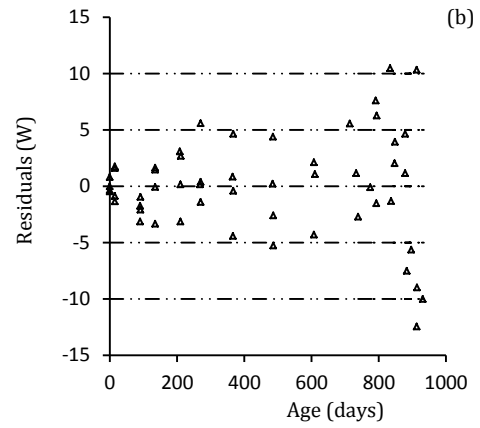
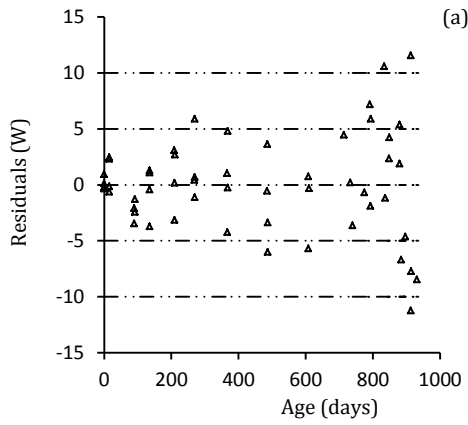




Figure 1. Absolute residuals ( $\Delta$ ) for some variables plotted against the time axis (Age, days). The residual plots are based on: (a) Liveweight ( $W$ , kg) described by Eqn (3) combined with Eqn (4); (b)  $W$  described by Eqn (2) with Eqn (5); (c) Abdominal fat ( $AbFat$ , kg) described by Eqn (1) with Eqn (4); (d)  $AbFat$  described by Eqn (1) with Eqn (6); (e) Carcass (kg) described by Eqn (3) with Eqn (4); (f) Carcass described by Eqn (2) with Eqn (5); (g) Blood (kg) described by Eqn (3) with Eqn (4); and (h) Blood described by Eqn (2) with Eqn (5). Details of equations are in the text.

Heading: Prediction of the long-term growth of goat wethers

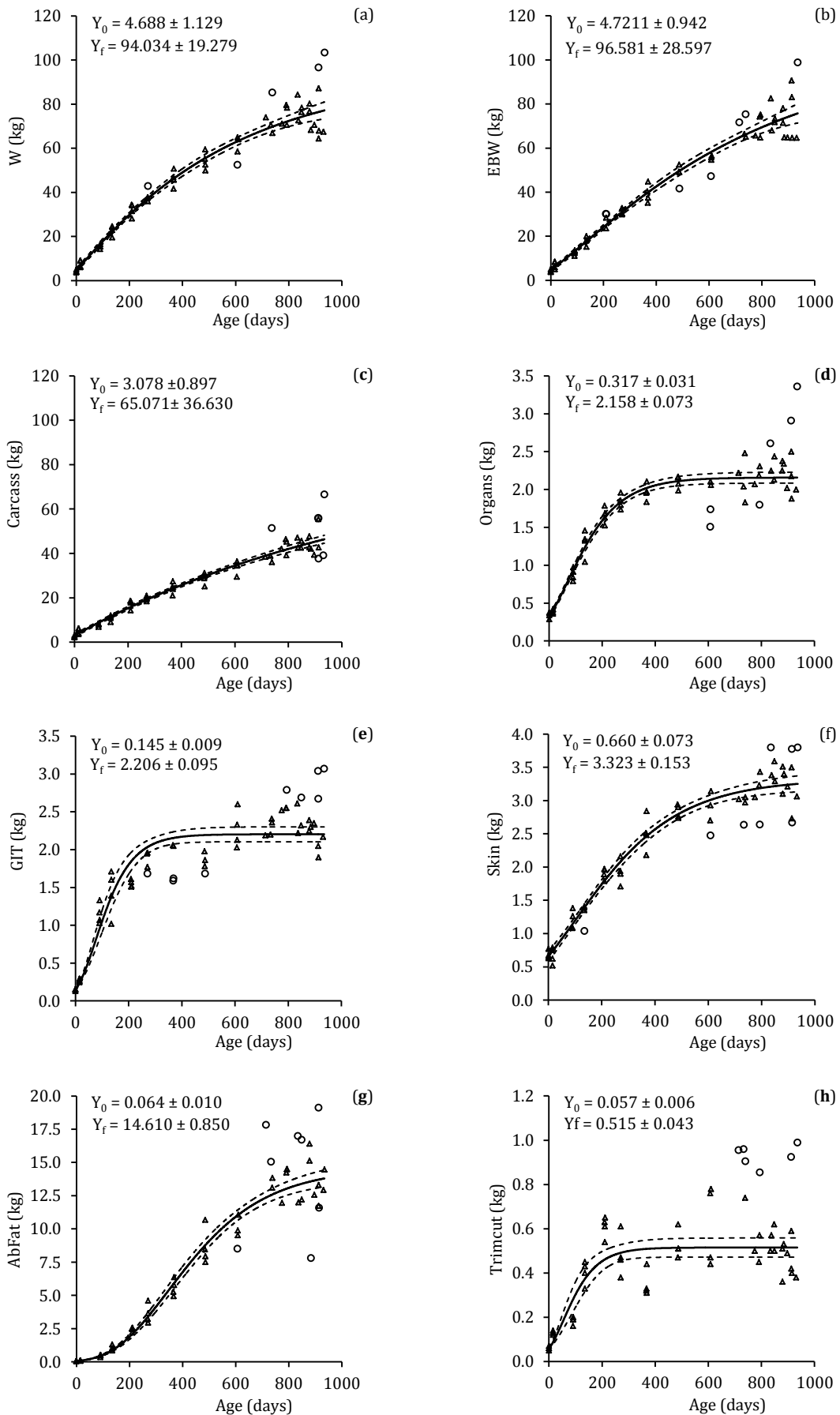


Figure 2. Observed ( $\Delta$ ), predicted (solid lines), 95% confidence interval (95%CI, dashed lines), and outlier (o) values of the growth profiles and 95%CI for the intercept and asymptotic estimates for the variables. Age (abscissa) is expressed in days (days). Dependent variables and the respective fitted models are: (a) liveweight ( $W$ , kg), Eqn (2) combined with Eqn (5); (b) empty body weight ( $EBW$ , kg), Eqn (2) with Eqn (5); (c) carcass weight ( $Carcass$ , kg), Eqn (2) with Eqn (5); (d) total weight of the organs ( $Organs$ , kg), Eqn (1) with Eqn (6); (e) weight of the gastrointestinal tract ( $GIT$ , kg), Eqn (1) with Eqn (6); (f) weight of the skin ( $Skin$ , kg), Eqn (1) with Eqn (5); (g) weight of the abdominal fat ( $AbFat$ , kg), Eqn (1) with Eqn (6); and (h) weight of the trimmed cuts ( $Trimcut$ , kg), Eqn (1) with Eqn (6). Details of equations are in the text.

Heading: Prediction of the long-term growth of goat wethers

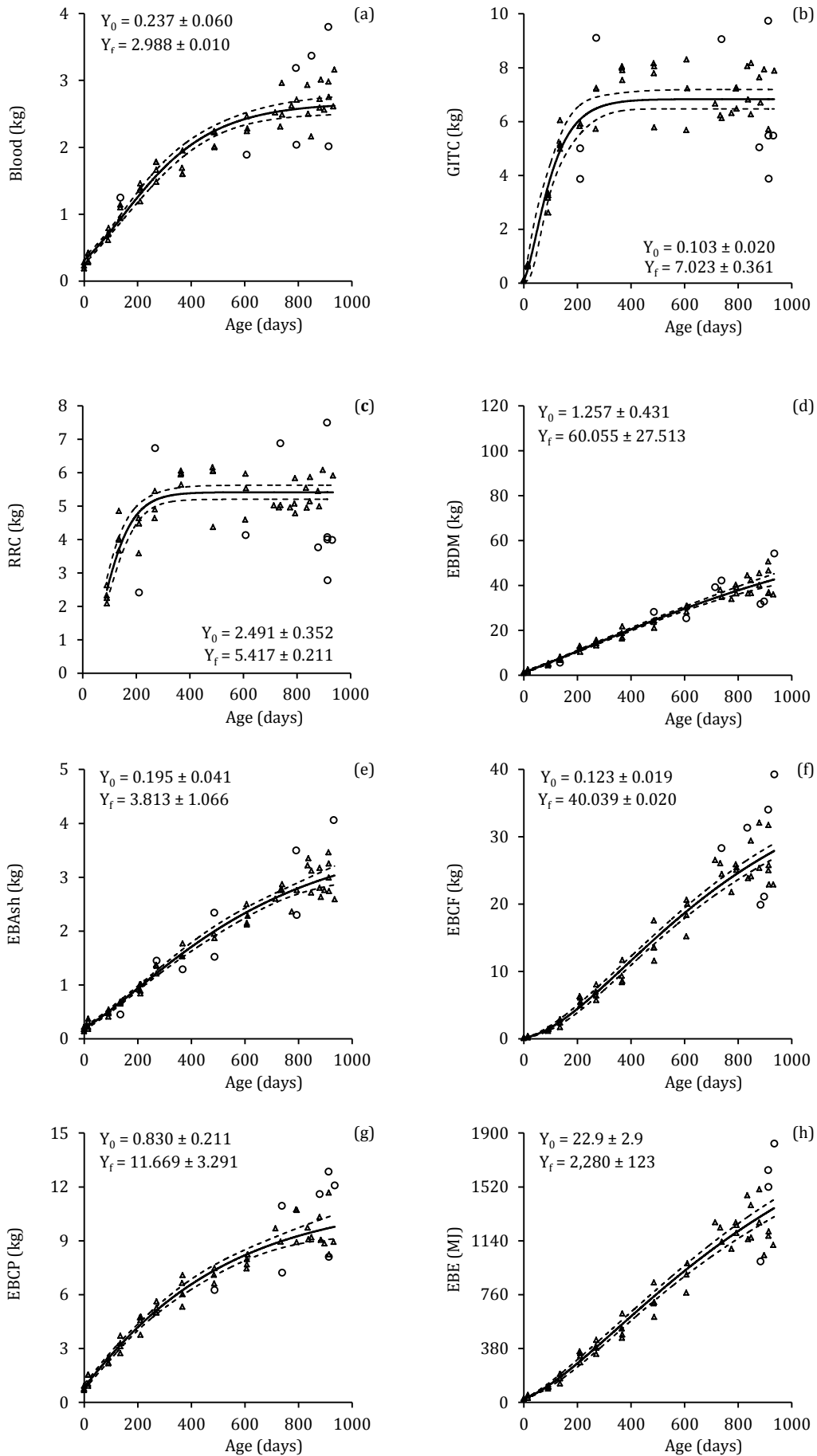


Figure 3. Observed ( $\Delta$ ), predicted (solid lines), 95% confidence interval (95%CI, dashed lines), and outlier (o) values of the growth profiles and 95%CI for the intercept and asymptotic estimates for the variables. Age (abscissa) is expressed in days (days). Dependent variables and the respective fitted models are: (a) Blood (*Blood*, kg), Eqn (2) combined with Eqn (5); (b) Gastrointestinal Tract content (*GITC*, kg), Eqn (2) with Eqn (6); (c) Ruminoreticular Content (*RRC*, kg), Eqn (1) with Eqn (4); (d) empty body dry matter (*EBDM*, kg), Eqn (2) with Eqn (5); (e) empty body ash (*EBAsh*, kg), Eqn (2) with Eqn (5); (f) empty body crude fat (*EBCF*, kg), Eqn (2) with Eqn (6); (g) empty body crude protein (*EBCP*, kg), Eqn (2) with Eqn (5); and empty body energy (*EBE*, MJ), Eqn (2) with Eqn (6). Details of equations are in the text.

Heading: Prediction of the long-term growth of goat wethers

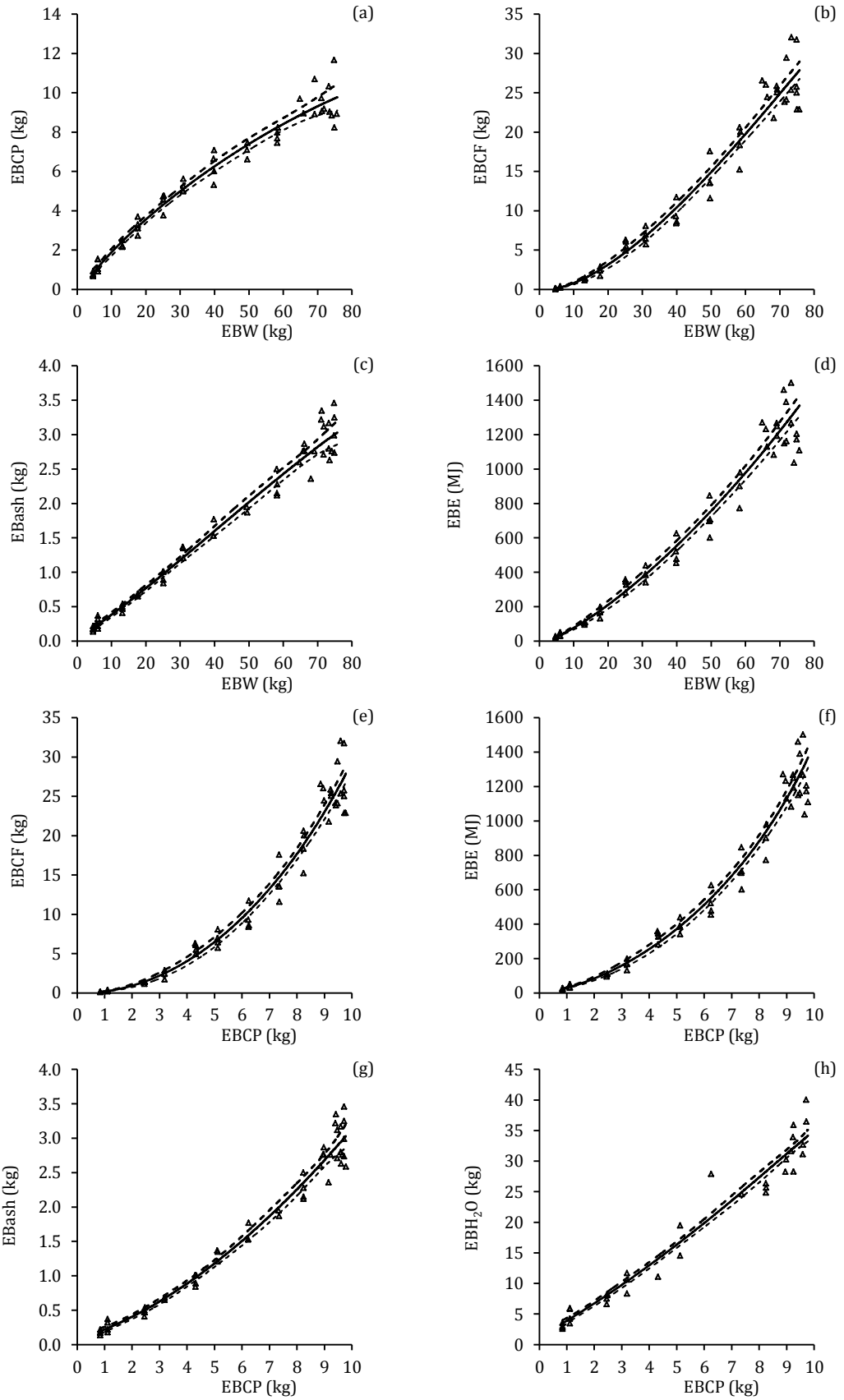


Figure 4. Observed ( $\Delta$ ) and predicted point (solid lines) and 95% interval (dashed lines) estimates for some variables plotted against the predicted empty body weight (*EBW*) and empty body crude protein (*EBCP*). On panels (a), (b), (c), and (d) are the respective plots of *EBCP* (kg), *EBCF* (kg), *EBAsh* (kg), and *EBE* (MJ) against *EBW* (kg). On panels (e), (f), (g), and (h) are the respective plots of *EBCF*, *EBE*, *EBAsh*, and *EBH<sub>2</sub>O* (kg) against the *EBCP*.

## 5. CONCLUSÕES

O modelo de richardz se ajusta a maioria dos perfis de crescimento de caprinos castrados por sua capacidade de mimetizar os modelos de brody, logístico e gompertz, dependendo da característica do perfil avaliado.

O modelo de gompertz somente é verossímil nos perfis que possuem característica sigmoide.

O modelo composto brody-gompertz deve ser avaliado com critério, principalmente quando se objetiva caracterizar um ponto de inflexão alternativo à puberdade, que ocorre normalmente no desmame de animais criados em sistema intensivo.

A determinação da estrutura de variância e covariância que melhor se ajusta a cada perfil avaliado sofre influência marcante das características de dispersão dos dados ao longo do tempo.

O crescimento das partes corporais e a composição do ganho de corpo vazio ao longo do tempo em caprinos castrados não são constantes em toda a gama de massa corporal estudada.

A fase assintótica dos perfis de crescimento não foi caracterizada para todas as variáveis analisadas, apesar do período longo de crescimento avaliado.



## 6. APÊNDICE

### DATABASE

data pavesi;

input trt age anim W EBW carcass organs GIT skin AbFat Trimcut blood GITC RRC EBDM EBash EBCF EBCP EBE

y=w;

t=Age;

Dataline

1	0	1	27.323	4.854	3.146	0.374	0.152	0.768	0.077	0.065	0.276	0.130	0.007	1.390	0.224	0.146	0.922	18.117
1	0	2	19.454	3.579	2.270	0.287	0.141	0.626	0.052	0.050	0.194	0.080	0.004	0.999	0.141	0.096	0.670	13.523
1	0	3	22.815	4.044	2.574	0.339	0.131	0.670	0.068	0.055	0.228	0.088	0.007	1.184	0.181	0.127	0.761	16.306
1	0	4	21.323	3.680	2.308	0.293	0.153	0.640	0.055	0.055	0.200	0.113	0.005	1.109	0.173	0.109	0.728	14.068
2	15	5	29.142	5.727	3.614	0.359	0.247	0.520	0.083	0.137	0.280	0.710	0.008	1.492	0.224	0.197	0.914	18.729
2	15	6	31.635	6.191	4.047	0.380	0.260	0.620	0.086	0.128	0.300	0.615	0.030	1.614	0.182	0.189	1.034	19.362
2	15	7	50.700	8.620	6.106	0.415	0.295	0.788	0.104	0.117	0.406	0.620	0.010	2.414	0.317	0.380	1.528	25.206
2	15	8	48.989	8.797	6.260	0.420	0.270	0.752	0.118	0.129	0.423	0.680	0.035	2.480	0.370	0.332	1.536	24.271
3	91	9	108.250	14.335	8.140	0.915	1.070	1.255	0.490	0.190	0.710	2.620	2.090	4.803	0.471	1.443	2.203	69.717
3	90	10	95.222	13.080	6.915	0.790	1.165	1.085	0.350	0.155	0.605	3.165	2.315	4.414	0.405	1.140	2.155	57.718
3	91	11	113.006	15.227	8.112	0.975	1.325	1.375	0.525	0.195	0.785	3.255	2.245	5.263	0.540	1.381	2.509	70.640
3	90	20	105.074	14.595	7.910	0.840	1.025	1.075	0.500	0.185	0.700	3.340	2.625	4.720	0.495	1.367	2.194	65.010
4	135	32	171.226	21.120	10.880	1.325	1.705	1.350	0.995	0.430	1.135	4.985	3.670	7.376	0.648	2.400	3.286	108.235
4	135	36	199.832	22.935	12.065	1.460	1.600	1.410	1.295	0.445	1.095	5.115	3.990	8.274	0.689	2.879	3.704	124.749
4	135	40	131.429	18.525	9.115	1.045	1.015	1.040	0.850	0.325	0.940	5.180	4.030	5.550	0.450	1.717	2.733	81.239
4	135	43	167.445	22.965	11.505	1.345	1.385	1.385	1.015	0.400	1.250	6.050	4.845	6.787	0.678	2.409	3.110	109.226
5	211	13	327.773	32.555	18.365	1.690	1.515	1.955	2.565	0.645	1.390	5.920	4.480	12.167	1.008	5.499	4.771	195.102
5	209	16	358.531	32.645	18.630	1.785	1.610	1.885	2.505	0.625	1.360	5.825	4.635	13.020	1.005	6.306	4.730	217.719
5	210	23	281.907	26.625	14.295	1.525	1.505	1.790	2.225	0.540	1.185	5.005	3.575	10.369	0.840	4.932	3.763	175.351
5	210	26	346.490	29.865	17.850	1.630	1.565	1.970	2.460	0.610	1.455	3.865	2.415	12.424	0.888	6.097	4.567	206.737
6	270	41	384.206	36.025	19.310	1.795	1.685	1.895	3.645	0.465	1.655	7.240	4.895	14.266	1.212	6.431	5.618	221.028
6	269	45	390.865	35.427	20.395	1.855	1.945	1.935	3.215	0.455	1.777	5.730	4.635	14.443	1.365	6.974	4.991	236.099
6	270	46	439.808	40.960	20.975	1.960	1.955	2.155	4.600	0.380	1.780	9.105	6.740	15.743	1.351	8.055	5.267	265.520
6	270	47	341.504	34.150	18.430	1.735	1.770	1.705	2.935	0.605	1.480	7.210	5.445	13.206	1.454	5.718	4.991	201.991
7	368	15	625.420	48.685	27.445	2.105	2.045	2.835	6.370	0.440	1.950	7.540	5.635	21.766	1.766	11.701	7.076	356.520
7	366	18	521.690	44.696	24.961	1.955	2.060	2.505	5.265	0.315	1.690	8.000	5.940	18.795	1.529	9.318	6.644	294.881

7	368	21	477.925	44.045	24.040	1.970	1.620	2.475	5.765	0.305	1.600	7.905	5.980	16.852	1.287	8.585	6.006	278.309
7	367	42	454.329	39.990	21.070	1.835	1.590	2.180	4.945	0.330	1.595	8.050	6.060	16.276	1.525	8.391	5.324	268.456
8	485	31	697.449	53.200	28.765	2.160	1.975	2.940	8.450	0.465	2.220	8.160	6.160	23.726	1.953	13.526	7.090	401.386
8	486	37	845.421	57.640	31.235	2.170	1.780	2.895	10.675	0.620	2.235	7.785	6.040	28.284	2.336	17.574	6.614	496.513
8	487	38	601.640	47.980	25.095	1.985	1.860	2.740	7.495	0.510	2.005	8.050	6.055	21.028	1.520	11.583	6.258	349.045
8	487	39	706.533	50.810	29.680	2.075	1.685	2.755	7.945	0.510	1.995	5.775	4.365	24.413	1.866	13.539	7.456	398.353
9	610	22	980.237	61.340	34.765	2.060	2.600	3.135	11.070	0.780	2.280	7.225	5.530	30.790	2.277	20.044	8.227	549.982
9	607	24	772.606	50.540	29.500	1.505	2.025	2.695	8.515	0.760	1.890	5.675	4.585	25.419	2.496	15.221	7.454	415.313
9	608	28	996.894	62.550	36.375	2.105	2.325	2.930	9.880	0.470	2.460	8.300	5.965	30.851	2.151	20.616	7.978	565.145
9	608	14	900.705	56.305	34.445	1.745	2.125	2.475	9.530	0.440	2.235	5.400	4.135	28.224	2.117	18.348	7.677	497.916
10	714	19	1270.537	71.735	38.510	2.220	2.190	3.020	17.825	0.955	2.515	6.655	5.020	39.207	2.602	26.557	9.694	708.680
10	739	7	1130.978	64.490	36.105	1.830	2.360	3.050	13.835	0.905	2.485	6.115	5.030	34.808	2.873	24.474	7.228	644.620
10	733	30	1232.592	68.245	38.970	2.040	2.200	2.635	15.055	0.960	2.305	6.230	4.955	38.014	2.758	26.036	8.947	689.424
10	738	29	1368.970	82.830	51.495	2.480	2.405	2.970	13.090	0.735	2.960	9.065	6.885	42.243	2.766	28.315	10.948	760.037
11	793	4	1193.521	67.960	39.135	1.805	2.545	2.640	14.480	0.570	2.040	7.260	5.840	36.413	2.300	25.057	8.922	657.271
11	794	5	1249.669	75.550	45.270	2.305	2.790	3.430	14.510	0.855	2.710	6.470	4.780	39.101	2.761	25.427	10.700	685.582
11	775	49	1082.321	68.610	41.995	2.070	2.515	3.050	11.945	0.495	2.615	6.305	4.960	33.943	2.356	21.771	9.690	590.781
11	791	6	1268.331	76.980	46.480	2.185	2.545	3.225	14.240	0.445	3.185	7.220	5.065	40.228	3.502	25.880	10.737	691.457
12	848	12	1390.770	74.035	42.565	2.130	2.315	3.585	16.715	0.615	2.160	6.265	5.135	42.305	2.711	29.444	9.983	772.707
12	849	2	1162.574	75.595	45.625	2.435	2.690	3.290	12.195	0.500	3.370	8.165	5.870	36.545	3.115	24.114	9.184	659.959
12	837	34	1150.151	70.315	42.710	2.245	2.220	3.375	11.995	0.570	2.500	6.820	4.950	36.425	3.352	23.868	9.066	646.738
12	834	44	1460.480	81.605	47.175	2.615	2.610	3.800	17.000	0.500	2.925	8.055	5.545	44.517	3.216	31.367	9.734	836.748
13	897	25	1037.688	68.215	39.390	2.020	2.345	3.205	12.560	0.485	2.560	7.925	6.075	32.860	2.760	21.138	8.845	574.009
13	884	33	994.071	65.895	42.105	2.340	2.300	3.400	7.805	0.530	3.005	6.695	4.990	31.708	2.631	19.909	9.044	557.840
13	879	51	1267.600	74.425	42.825	2.375	2.250	3.505	15.140	0.355	2.585	7.640	5.450	40.217	3.169	25.346	11.603	686.424
13	879	50	1502.117	77.770	47.710	2.250	2.385	3.095	16.395	0.510	2.715	5.040	3.770	45.355	2.797	32.071	10.330	838.894
14	912	52	1638.836	93.555	55.910	2.915	3.040	3.495	19.130	0.925	3.800	9.740	7.500	50.602	3.458	34.051	12.847	911.363
14	914	48	1205.276	65.920	42.665	1.880	1.895	2.670	11.595	0.400	2.745	3.880	2.780	36.860	2.741	25.768	8.231	676.847
14	931	8	1108.670	65.245	39.105	2.000	2.165	3.060	12.930	0.375	2.610	5.115	3.990	35.983	4.055	22.893	8.931	614.285
14	913	53	1520.316	84.425	55.395	2.500	2.675	3.775	13.310	0.585	2.980	5.715	4.005	46.600	2.992	31.739	11.666	840.940
14	913	17	1173.512	62.250	37.665	2.175	2.050	2.725	11.730	0.415	2.015	5.480	4.070	36.529	3.250	25.030	8.112	671.187
14	935	3	1825.544	100.340	66.605	3.365	3.070	3.800	14.460	0.990	3.160	7.885	5.905	54.244	2.591	39.258	12.081	1050.885

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class trt anim;
model y=trt/ddfm=kr outp=baiano;
repeated /type=vc subject=anim group=trt;
run;
/*Gompertz model*/
proc nlmixed data=pavesi tech=newrap maxit=500;
parms
w0=1 to 15 by 1
m=.01 to .1 by .01
d=.001 to .01 by .001
s0=1000 to 40000 by 500
c=.01 to .1 by .01
/best=1;
bounds w0>0, m>0, d>0, s0>0, c>0;
v=s0*exp(c*t);
mean=w0*exp(m*(1-exp(-d*t))/d);
/*inflection point*/
ti=(1/d)*log(m/d);
meanti = w0*exp(m*(1-exp(-d*ti))/d);
estimate 'delta1' meanti;
/*Average daily rate of retention*/
Mfinal=w0*exp(m/d);
M0=w0;
estimate 'M0' M0;
estimate 'Mfinal' Mfinal;
mean=w0*exp(m*(1-exp(-d*t))/d);
mean15=w0*exp(m*(1-exp(-d*15))/d);
mean90=w0*exp(m*(1-exp(-d*90))/d);
mean210=w0*exp(m*(1-exp(-d*210))/d);
mean365=w0*exp(k2*(1-exp(-d*365))/d);
mean730=w0*exp(k2*(1-exp(-d*730))/d);
mean900=w0*exp(k2*(1-exp(-d*900))/d);
estimate 'delta1' (mean15-M0)/(15-0);
estimate 'delta2' (mean90-mean15)/(90-15);
estimate 'delta3' (mean210-mean90)/(210-90);
estimate 'delta4' (mean365-mean210)/(365-210);
estimate 'delta5' (mean730-mean365)/(730-365);
estimate 'delta6' (mean900-mean730)/(900-730);
resid=y-mean;
id resid;
model y ~ normal(mean,v);
predict mean ti out=raphael;
run;
quit;
proc print data=raphael;
var t y pred lower upper;
run;
quit;
proc gplot data=raphael;
plot y*t pred*t lower*t upper*t/frame overlay;
plot resid*t/frame overlay;
plot resid*y/frame overlay;
plot der1*t/frame overlay;
plot der2*t/frame overlay;
run;
quit;
/*Richards model*/
proc nlmixed data=pavesi tech=newrap maxit=500;

```

```

parms
Y0=150 to 350 by 50
Yf=2000 to 3500 by 100
n=-1 to 1 by .1
k=.0001 to .001 by .0001
s0=200 to 1000 by 100
c=.00001 to .0001 by .00001
sb=100000 to 200000 by 10000
/best=1;
bounds Y0>0, Yf>0, n>=-1, n<=1, k>0, s0>0, sb>0, c>0;
v=s0;
v=s0*exp(c*t);
v=s0+sb*(1-exp(-c*t));
mean=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*t))**(1/n);
/*inflection point*/
ti=-(1/k)*log(n*y0**n/(yf**n-y0**n));
meanti=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*ti))**(1/n);
estimate 'delta1' meanti;
/*Average daily rate of retention*/
Mfinal=Yf;
M0=Y0;
estimate 'M0' M0;
estimate 'Mfinal' Mfinal;
mean0=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*0))**(1/n);
mean15=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*15))**(1/n);
mean90=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*90))**(1/n);
mean210=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*210))**(1/n);
mean365=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*365))**(1/n);
mean730=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*730))**(1/n);
mean900=Y0*Yf/(Y0**n+(Yf**n-Y0**n)*exp(-k*900))**(1/n);
estimate 'delta1' (mean15-mean0)/(15-0);
estimate 'delta2' (mean90-mean15)/(90-15);
estimate 'delta3' (mean210-mean90)/(210-90);
estimate 'delta4' (mean365-mean210)/(365-210);
estimate 'delta5' (mean730-mean365)/(730-365);
estimate 'delta6' (mean900-mean730)/(900-730);
resid=y-mean;
id resid;
model y ~ normal(mean,v);
predict mean ti out=raphael;
run;
quit;
proc print data=raphael;
var t y pred lower upper;
run;
quit;
proc gplot data=raphael;
plot y*t pred*t lower*t upper*t/frame overlay;
plot resid*t/frame overlay;
plot resid*y/frame overlay;
plot der1*t/frame overlay;
plot der2*t/frame overlay;
run;
quit;
/*Brody-Gompertz model*/
proc nlmixed data=pavesi tech=newrap ;
parms
Yf1=-100 to 30 by 10
Y10=-100 to 10 by 10

```

```

k1=1 to 5 by .5
Y20=5 to 50 by 5
k2=.0001 to .001 by .0001
d=.0001 to .001 by .0001
s0=1 to 3 by .5
c=.00001 to .0001 by .00001
sb=200 to 1500 by 200
/best=1;
bounds Yf1>-101, Y10>-101, k1>0, Y20>0, k2>0, d>0, s0>0, sb>0, c>0;
v=s0;
v=s0*exp(c*t);
v=s0+sb*(1-exp(-c*t));
mean=Yf1-(Yf1-Y10)*exp(-k1*t) + Y20*exp(k2*(1-exp(-d*t)))/d);
/*Average daily rate of retention*/
Mfinal=Yf1+Y20*exp(k2/d);
M0=Y10+Y20;
estimate 'M0' M0;
estimate 'Mfinal' Mfinal;
mean=Yf1-(Yf1-Y10)*exp(-k1*t) + Y20*exp(k2*(1-exp(-d*t)))/d);
mean15=Yf1-(Yf1-Y10)*exp(-k1*15) + Y20*exp(k2*(1-exp(-d*15)))/d);
mean90=Yf1-(Yf1-Y10)*exp(-k1*90) + Y20*exp(k2*(1-exp(-d*90)))/d);
mean210=Yf1-(Yf1-Y10)*exp(-k1*210) + Y20*exp(k2*(1-exp(-d*210)))/d);
mean365=Yf1-(Yf1-Y10)*exp(-k1*365) + Y20*exp(k2*(1-exp(-d*365)))/d);
mean730=Yf1-(Yf1-Y10)*exp(-k1*730) + Y20*exp(k2*(1-exp(-d*730)))/d);
mean900=Yf1-(Yf1-Y10)*exp(-k1*900) + Y20*exp(k2*(1-exp(-d*900)))/d);
estimate 'delta1' (mean15-M0)/(15-0);
estimate 'delta2' (mean90-mean15)/(90-15);
estimate 'delta3' (mean210-mean90)/(210-90);
estimate 'delta4' (mean365-mean210)/(365-210);
estimate 'delta5' (mean730-mean365)/(730-365);
estimate 'delta6' (mean900-mean730)/(900-730);
resid=y-mean;
id resid;
model y ~ normal(mean,v);
predict mean ti out=raphael;
run;
quit;
proc print data=raphael;
var t y pred lower upper;
run;
quit;
proc gplot data=raphael;
plot y*t pred*t lower*t upper*t/frame overlay;
plot resid*t/frame overlay;
plot resid*y/frame overlay;
plot der1*t/frame overlay;
plot der2*t/frame overlay;
run;
quit;

```